

# **2017 IEEE 24th Symposium on Computer Arithmetic (ARITH 2017)**

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# 2017 IEEE 24th Symposium on Computer Arithmetic

## ARITH 2017

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