

---

# SpecExec: Massively Parallel Speculative Decoding for Interactive LLM Inference on Consumer Devices

---

Ruslan Svirschevski\*†♡ Avner May\*♣ Zhuoming Chen\*‡

Beidi Chen‡◇ Zhihao Jia‡ Max Ryabinin\*♦

† Yandex ♡ HSE University ♣ Together AI ♦ Carnegie Mellon University ◇ Meta AI

ruslansv@gmail.com, avner@together.ai, zhuominc@andrew.cmu.edu,

{zhihaoj2,beidic}@andrew.cmu.edu, mryab@together.ai

## Abstract

As large language models gain widespread adoption, running them efficiently becomes a crucial task. Recent works on LLM inference use speculative decoding to achieve extreme speedups. However, most of these works implicitly design their algorithms for high-end datacenter hardware. In this work, we ask the opposite question: *how fast can we run LLMs on consumer machines?* Consumer GPUs can no longer fit the largest available models and must offload them to RAM or SSD. With parameter offloading, hundreds or thousands of tokens can be processed in batches within the same time as just one token, making it a natural fit for speculative decoding. We propose SPECEXEC (Speculative Execution), a simple parallel decoding method that can generate up to 20 tokens per target model iteration for popular LLM families. SpecExec takes the most probable continuations from the draft model to build a “cache” tree for the target model, which then gets validated in a single pass. Using SpecExec, we demonstrate inference of 50B+ parameter LLMs on consumer GPUs with RAM offloading at 4–6 tokens per second with 4-bit quantization or 2–3 tokens per second with 16-bit weights.<sup>1</sup>

## 1 Introduction

Open-access large language models (LLMs), such as Llama [Touvron et al., 2023] and Mistral [Jiang et al., 2023], have become increasingly capable in the past years, and their adoption has grown dramatically. Although these models are openly available, users who are interested in running these models on consumer-grade GPUs (for example, due to privacy or cost reasons) face significant challenges. Many open-access LLMs are too large to fit on consumer GPUs, which necessitates offloading them onto CPU RAM to perform inference. Given the limited memory bandwidth between the CPU and the GPU, as well as the fact that all model parameters must be transferred to the GPU for the LLM to generate each new token, offloading is extremely slow and bandwidth-bound. For example, generating a single token using Llama 2-70B in 16 bit with offloading on an RTX 3090 GPU takes at least 4.5 seconds<sup>2</sup>.

A recent line of work that aims to speed up LLM inference is speculative decoding [Leviathan et al., 2023, Chen et al., 2023a], which uses a small draft model to predict the next tokens and a larger target model to verify which of those tokens to accept in parallel. Although speculative decoding is a promising direction, the speedups that existing methods can attain in the offloading setting are relatively modest. While studying existing approaches [Leviathan et al., 2023, Miao et al., 2023, Sun et al., 2023], we discovered that these methods do not scale well with the draft model token budget. In particular, as shown in Figure 1 (left), the number of tokens accepted by the target model is

---

<sup>\*</sup>Equal contribution.

<sup>1</sup>The code is available at [github.com/yandex-research/specexec](https://github.com/yandex-research/specexec).

<sup>2</sup>Assuming PCIe-4.0 and at least 140GB of DDR5 RAM with an efficient offloading implementation.

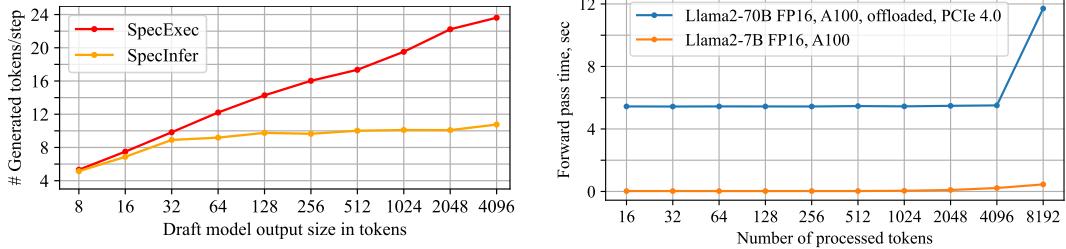


Figure 1: Acceptance counts vs draft size (left), forward pass GPU time vs input size (right). Llama 2-7B draft model, offloaded Llama 2-70B target model, MTBench dataset,  $t=0.6$  and  $\text{top-p}=0.9$ .

empirically upper-bounded (approximately by 10 for this model and dataset combination) regardless of the number of speculated tokens. In turn, methods that scale better with more draft tokens Chen et al. [2024a] rely on static tree structures that may not be optimal for every setting, as they require tree structure optimization for every change in the text domain, generation parameters, and the hardware setup.

In this work, we aim to improve the effectiveness of speculative decoding for running large language models on consumer hardware with RAM offloading. We propose SpecExec, a speculative decoding method that addresses the performance, flexibility and scalability issues of prior methods. SpecExec<sup>3</sup> adopts a powerful draft model to deterministically<sup>4</sup> construct a large draft tree that covers the most likely continuations of the prefix with a parallel search algorithm. We then apply a simple verification algorithm that views this tree as a cache of potential continuations and validates it with the target model in a single pass.

Our main contributions can be summarized as follows:

1. We analyze the empirical behavior of speculative decoding algorithms with large language models and identify ways to improve their acceptance rate when scaling to thousands of draft tokens.
2. We propose SpecExec — a speculative decoding algorithm that improves the structure of generated draft trees for very large token budgets. We demonstrate that this technique can produce draft trees resulting in 10–20 accepted tokens with sufficiently large budgets.
3. Using our observations and SpecExec, we design a system that can run Llama 2-70B or comparable models interactively at 4–6 tokens/second using 4-bit quantization or 2–3 tokens/second with 16-bit weights on consumer GPUs with offloading, with 10–18x speedups compared to sequential inference on the same hardware.

## 2 Background

### 2.1 Speculative Decoding

In this study, we extend a family of algorithms for speculative decoding of autoregressive LLMs Stern et al. [2018], Leviathan et al. [2023], Chen et al. [2023a]. These algorithms generate tokens in two phases: *drafting* and *verification*.

During the drafting phase, the algorithm generates a candidate sequence of tokens by sampling from a small *draft model*  $P(x_{t+1}|x_{0:t}, \theta_{\text{draft}})$ . In turn, the verification stage leverages the *target model*  $P(x_{t+1}|x_{0:t}, \theta_{\text{main}})$  to verify these draft sequences and accept all tokens that have passed the verification. The probability of accepting a token is chosen in a way that preserves the output distribution of sequential sampling from the original LLM Leviathan et al. [2023], Chen et al. [2023a], Sun et al. [2023]. A key advantage of speculative algorithms is that the main model can verify *all* draft tokens in parallel, which is more efficient than sequentially generating one token at a time.

<sup>3</sup>We chose this name because our method directly applies speculative execution to LLM inference. The draft model “guesses” which token prefixes the target model will need to continue, and then the target model computes distributions of continuations with a single forward pass on the speculated prefix tree.

<sup>4</sup>In contrast, speculative sampling requires stochastic generation of the draft tree using draft probabilities.

Subsequent works in speculative decoding extend this idea in several directions, including generating multiple draft sequences or draft trees, using multiple draft models, and finetuning the draft models to improve generation speed Miao et al. [2023], Liu et al. [2023], Xu et al. [2023]. Another line of follow-up studies explores alternative sources for the draft model: namely, self-speculative decoding uses a subset of main model layers to produce a draft Zhang et al. [2023], REST retrieves draft sequences from a search index He et al. [2023], and staged speculative decoding uses multiple levels of speculation Spector and Re [2023]. Leveraging these techniques, practitioners have built efficient implementations for fast LLM inference [Miao et al., 2023, Cai et al., 2023]. We refer the readers to survey papers for a more detailed coverage of speculative decoding methods Zhang et al. [2024a], Xia et al. [2024a].

In our analysis, we focus on speculative decoding algorithms that support sampling from the target model and guarantee identical sample probabilities vs standard generation. The rationale for our choice is that most popular LLM applications (such as chat assistants) require stochastic sampling to introduce variability into their responses. This focus rules out several algorithms that only support greedy inference Fu et al. [2023], Liu et al. [2023]. Still, most works on speculative decoding fit within that criterion.

## 2.2 Parameter Offloading

Another recent line of work explores running and training large models with limited accelerator memory by “offloading” their parameters to more abundant storage, such as RAM or even SSD [Pudipeddi et al., 2020, Ren et al., 2021, Alizadeh et al., 2023]. This technique works by loading model parameters on the GPU when they are needed for computation. Since most deep learning models use layers in a fixed order, offloading can pre-dispatch the next layer’s parameters in the background.

This technique works particularly well when processing large batches of data, during training Pudipeddi et al. [2020], Ren et al. [2021] or large-batch non-interactive inference Aminabadi et al. [2022], Sheng et al. [2023], where each layer process multiple tokens each time it is loaded. In turn, when doing interactive inference, offloading works significantly slower than on-device inference. This is because interactive inference has to process one or few tokens at a time, and therefore spends most of the time waiting for the parameters to load.

## 2.3 Running LLMs on Consumer Devices

While our observations are not specific to any particular LLM, we focus on a practical case of running modern instruction-tuned models such as Llama-2-70B-chat Touvron et al. [2023] and Mixtral 8x7B Jiang et al. [2024]. To better estimate the target hardware setups, we study communities dedicated to running large models locally, such as LocalLlama [2023]. A popular<sup>5</sup> hardware configuration for running those models locally is a desktop or a cloud instance with a single consumer-grade GPU<sup>6</sup> with 12–24 GB VRAM, 4–8 CPU cores, 32–64 GB RAM, and a PCIe 3.0 or 4.0 x16 bus between CPU and GPU. Another popular setup is devices without a dedicated GPU, such as MacBooks with an ARM-based CPU, 16 GB RAM, and an SSD. While this survey may not be fully representative, it reveals popular setups that are not targeted by most speculative decoding research.

Running the largest language models in this setup requires either extreme compression or offloading. While it is possible to fit 70B+ models into consumer GPUs by compressing them to 1.5–2 bits per parameter Chee et al. [2023], Tseng et al. [2023], doing so causes significant accuracy losses that defeat the purpose of running large models Dettmers and Zettlemoyer [2022], Tseng et al. [2023]. Thus, practitioners with consumer-grade hardware may find it optimal to run 50B+ models with mild (e.g. 4-bit) quantization and offload parameters from GPU to RAM or SSD Alizadeh et al. [2023].

## 3 Preliminary analysis

Speculative decoding with offloading benefits from the fact that it is more efficient to process tokens in parallel than sequentially. In conventional inference, this is caused by the higher arithmetic intensity

<sup>5</sup>Based on popular hardware guides such as Dettmers [2023] as well as setups examples (see A, B, C, D)

<sup>6</sup>For example, RTX 4060 or 4090 desktops, T4 or A2 VMs.

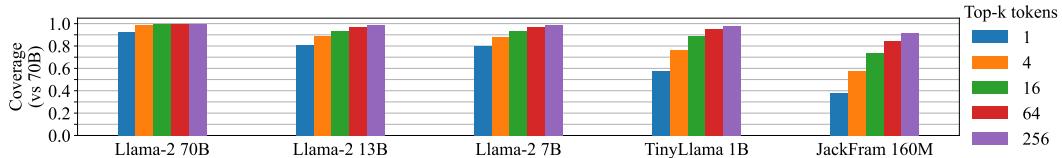


Figure 2: Llama-2 70B Chat model cumulative probability of most likely tokens compared to the draft model choice (all Llama draft models are chat versions), OASST1 dataset.

of GPU processing<sup>7</sup>. With offloading, there is a different bottleneck — loading model parameters from storage. Since offloading engines can dispatch model parameters in parallel with computation, the total processing time is the maximum of the time to load all parameters and the total computation time. In preliminary experiments (see Figure 1, right), we found that 70B models running on a consumer desktop can process thousands of tokens within nearly the same time as just a single token.

This leads us to a question: **how does speculative decoding perform when given hundreds to thousands of draft tokens?** As shown in concurrent work Chen et al. [2024a], speculative decoding algorithms with single or multiple sequences, like SpecInfer, are effectively upper-bounded in the number of accepted tokens as the speculation budget grows. This is confirmed by our observations (see Figure 1, left), where the number of accepted tokens saturates even for the more powerful Llama-2 7B.

In regular GPU inference, using 7B draft models would be impractical, as the drafting steps would take too long. However, in our setting, large draft models can be justified because each offloaded forward pass takes significantly more than a second (see Figure 1, right). This runs contrary to a popular intuition in speculative decoding that favors smaller draft models Miao et al. [2023], Liu et al. [2023].

We also observe that sampling from modern LLMs often results in a few high-probability tokens that add up nearly to a probability of 1 (see Figure 2 for an illustration). If we can find these tokens using the draft model, we can construct a draft that will be accepted with a similarly high probability. In preliminary experiments for 70B models, we found that running beam search with a capable draft model (e.g., Llama-2 7B) can recover many of these high-probability tokens. Unfortunately, this kind of deterministic search is incompatible with speculative decoding for stochastic sampling, which called for alternative validation method.

## 4 Method

### 4.1 Speculative Execution

As we observed in Section 3, high-probability continuations of large models are concentrated in a few tokens, and offloading benefits from running target model on hundreds or thousands of tokens. To use these observations, we formulate an alternative, simpler speculative decoding strategy. Unlike speculative decoding, SpecExec (short for “Speculative Execution”) does not propose a new sampling procedure: it runs standard (sequential) sampling while trying to “guess” which probabilities will be needed during future steps and precomputing these continuations *in parallel*. This is similar to speculative execution [Lampson, 2006] in modern CPUs that predicts which operations should be computed ahead of time to better utilize the compute cycles.

More specifically, whenever SpecExec uses target model probabilities, it looks them up in a speculative “cache”. If it encounters a token that is not in the cache, it queries the target model for that token and simultaneously computes probabilities for  $B$  potential **future** tokens chosen with the draft model, where  $B$  is the batch size. If the draft model can guess the likely next tokens accurately enough, the algorithm will be able to run multiple sampling iterations using these cached probabilities **without querying the target model** until it “exhausts the cache” and begins anew. A formal description of SpecExec is given in Algorithm 1.

To choose which future tokens should be precomputed, we run a search algorithm with the draft model to find  $B$  most likely tokens according to their cumulative probability  $\prod_t P(x_{t+1}|x_{0:t}, \theta_{\text{draft}})$ .

<sup>7</sup>Parallel matrix multiplications do more useful computations per memory access for multiple tokens.

---

**Algorithm 1** SPECULATIVE EXECUTION

---

```
1: Input: prompt  $x$ , models  $\theta_{\text{target}}$ ,  $\theta_{\text{draft}}$ , output length  $L$ , budget  $K$ , max depth  $D$ , batch size  $B$ 
2: Output: a sequence of  $L$  tokens generated by  $\theta_{\text{target}}$ 
3:  $\text{cache} := \text{PRECOMPUTE}(x, \theta_{\text{draft}}, \theta_{\text{target}}, K, D, B)$   $\triangleright$  target model probabilities for
   likely future tokens
4: for  $t = 1, 2, \dots, L$  do
5:   if  $x \notin \text{cache}$  then
6:      $\text{cache} := \text{PRECOMPUTE}(x, \theta_{\text{draft}}, \theta_{\text{target}}, K, D, B)$ 
7:      $p_{\text{target}} := \text{cache}[x]$   $\triangleright p_{\text{target}}$  is equal to  $P(\cdot | x_1, \dots, x_t, \theta_{\text{target}})$ 
8:      $x_{\text{next}} \sim \text{SAMPLE}(p_{\text{target}})$ 
9:      $x := x \oplus \{x_{\text{next}}\}$   $\triangleright$  append token
10:  return  $x$ 
11:
12: function  $\text{PRECOMPUTE}(x, \theta_{\text{target}}, \theta_{\text{draft}}, K, D, B)$ 
13:    $\tau := \text{CREATEDRAFTTREE}(x, \theta_{\text{draft}}, K, D, B)$   $\triangleright \tau$  is a tree with  $K$  tokens up to depth  $D$ 
14:    $\text{next\_probs} := \text{FORWARD}(\tau, \theta_{\text{target}})$   $\triangleright$  process  $\tau$  tokens in parallel with offloading;
   note:  $\text{next\_probs}$  is a matrix  $\in \mathbb{R}^{K \times \text{vocab}}$ 
15:    $\text{cache} := \{\}$ 
16:   for  $x_i \in \tau$  do
17:      $x_{\text{prefix}} := \pi(x_i, \tau)$   $\triangleright$  prefix in tree  $\tau$ 
18:      $\text{cache}[x_{\text{prefix}} \oplus \{x_i\}] = \text{next\_probs}[x_i]$   $\triangleright$  probabilities of possible next tokens
19:   return  $\text{cache}$ 
```

---

The details of the search algorithm are given in Section 4.2; unlike drafting with regular speculative decoding, this procedure is deterministic and always selects tokens with the highest probability.

**Comparison to speculative decoding.** The core advantage of SpecExec over regular speculative decoding is that the algorithm does not need the draft tree to follow a known probability distribution. In other words, SpecExec produces correct samples with any draft tree, even if it is deterministic. We use this property to construct the best possible speculative tree in ways that would break the assumptions of standard speculative decoding. For instance, our tree construction procedure, outlined in Section 4.2, considers only the most likely draft tokens and aims to capture a larger portion of the total probability mass.

However, this advantage comes at the cost of lower acceptance rates for any individual token. Algorithm 1 accepts a token  $x_t$  with probability  $P(x_{t+1} | x_{0:t}, \theta_{\text{target}})$ , because accepting a token with SpecExec is equivalent to sampling that token from the target model distribution. Meanwhile, the original speculative decoding (for example, Miao et al. [2023]) accepts tokens with a higher probability  $P(x_{t+1} | x_{0:t}, \theta_{\text{target}}) / P(x_{t+1} | x_{0:t}, \theta_{\text{draft}})$ .

For a small number of draft tokens (for instance, just one token), SpecExec is less effective than traditional speculative decoding. However, as we increase the number of draft tokens, speculative execution generates better-structured trees, which in practice leads to accepting more tokens for the same draft size; we verify this in Section 5.2.

**Correctness.** Next, we need to verify that SpecExec is equivalent to sequential sampling from the target model. Notably, unlike Leviathan et al. [2023], SpecExec does not change the probabilistic sampling procedure. The difference between SpecExec and sequential decoding is that SpecExec precomputes some probabilities, thus improving the GPU utilization in the case of offloading.

From a formal perspective, we rely on the fact that a speculative generation algorithm is equivalent to sequential sampling if it is locally equivalent in every node Miao et al. [2023]; in other words, it samples from the same probabilities for every prefix in the draft tree. Since SpecExec explicitly samples from the same probabilities as the main model, this is true by construction.

The fact that SpecExec follows the same sampling procedure has another side effect. If we view SpecExec as a deterministic function that depends on a pseudo-random number generator as input, we can prove a stronger degree of equivalence. Namely, for every seed value of the random number generator, SpecExec produces exactly the same outputs as sequential sampling with the same seed. In

contrast, speculative decoding does not have this properly, as it only guarantees correct probabilities for the overall generation procedure.

## 4.2 Search for the Optimal Draft Tree

As we discussed above, our algorithm uses the draft model to build a tree  $\tau$  of likely future tokens for speculative caching. In this section, we describe how to find these tokens efficiently. From an optimization perspective, we seek to construct a tree that will lead to the highest expected number of generated (accepted) tokens. This problem can be solved by viewing the tree construction as the search for the set of nodes (i.e., tokens) that have the highest cumulative probability with respect to the target model. As we show in Appendix A, this search can be reduced to the single-source shortest path (SSSP) search problem that can be solved efficiently using a modified version of the Dijkstra's algorithm Dijkstra [1959], described formally in Algorithm 2.

In summary, SpecExec follows a loop:

1. Run Algorithm 2 with the draft model to select  $K$  best tokens,
2. Process them with the target model using offloading,
3. Follow Algorithm 1 to determine which tokens are accepted.

For a visual high-level representation of the SpecExec algorithm, see Appendix B.

While Algorithm 2 is a rather special case of SSSP over a combinatorially large tree (the tree of all token sequences up to length  $K$ ), the general SSSP problem is well studied in the computer science community (see Appendix C). Therefore, practitioners will be able to leverage existing algorithms to implement Speculative Execution for a broad range of setups, including GPUs, mobile CPUs, or distributed systems.

---

### Algorithm 2 PARALLEL SSSP FOR DRAFTING

---

```

1: Input: prefix  $x$ ,  $\theta_{\text{draft}}$ , budget  $K$ , depth  $D$ , batch  $B$ 
2: Output: a tree of  $K$  likely future tokens
3:
4: function CREATEDRAFTTREE( $x, \theta_{\text{draft}}, K, D, B$ )
5:    $\tau := \text{TREE}(\{x\})$                                  $\triangleright$  an empty tree with root at  $x$ 
6:    $T := \infty$                                           $\triangleright$  stopping threshold
7:    $H := \text{PRIORITYQUEUE}(\{x : 0\})$   $\triangleright x$  has priority 0;  $H$  is ordered by negative
   cumulative log-probabilities
8:   for  $d = 1, 2, \dots, D$  do
9:      $\text{batch} := \emptyset$ 
10:    for  $b = 1, 2, \dots, B$  do
11:       $H, x_b, nll_b := \text{EXTRACTMIN}(H)$ 
12:      if  $nll_b < T$  then
13:         $\tau := \text{ADDCHILD}(\tau, x_b, nll_b)$ 
14:         $\text{batch} := \text{batch} \cup \{x_b\}$ 
15:      if  $\text{batch} = \emptyset$  then
16:        break
17:      if  $\text{SIZE}(\tau) \geq K$  then
18:         $T := -K \text{THCUMULATIVELOGPROB}(\tau, K)$   $\triangleright$  ignore tokens that fall outside the budget
19:         $\text{probs} := \text{FORWARD}(\text{batch}, \theta_{\text{draft}})$   $\triangleright$  run  $\theta_{\text{draft}}$  w/o offloading, attend to past tokens;
           note:  $\text{probs}$  is a matrix  $\in \mathbb{R}^{B \times \text{vocab}}$ 
20:         $\text{topk} := \text{SELECTBEST}(\text{batch}, \text{probs}, \tau, K)$   $\triangleright$  select best tokens by cumulative probability
21:        for  $(x_i, p_i) \in \text{topk}$  do
22:           $\log p_{\text{prefix}} := \text{CUMULATIVELOGPROB}(x_i, \tau)$   $\triangleright \sum_{x_t \in \pi(x_i, \tau)} \log P(x_t | \pi(x_t, \tau, \theta_{\text{draft}}))$ 
23:           $nll := -\log p_{\text{prefix}} - \log p_i$ 
24:           $H := \text{INSERT}(H, x_i, nll)$ 
25:         $H := \text{TRIM}(H, K)$                                           $\triangleright$  remove all except K best
26:    return  $\text{TRIM}(\tau, K)$ 

```

---

### 4.3 Implementation Details

Finally, we leverage several important technical improvements that speed up inference in real-world conditions. When running the forward pass with an offloaded target model, we accelerate inference by loading the next layer parameters in parallel with computing the previous layer activations using a dedicated CUDA stream, which is known to speed up offloading in other use cases Pudipeddi et al. [2020], Ren et al. [2021], Aminabadi et al. [2022]. We also preload the first few layers of the target model on the GPU in the background while drafting for a further speedup. We describe additional implementation details in Appendix D.

In our experiments, we also consider quantizing target models using recent post-training quantization algorithms Frantar et al. [2022], Lin et al. [2023], Dettmers et al. [2023]. While quantization is generally popular among LLM practitioners, it is particularly useful for our use case, as quantized models take less time to load from RAM to GPU and have RAM offloading requirements attainable by consumer hardware.

## 5 Experiments

### 5.1 Probability Coverage

The core assumption behind Algorithm 1 is that a reasonably large draft can “cover” most of the high-probability sequences of the target model. This is only possible if the target model predictions have low entropy (i.e., there is a small number of tokens with high probability) and the draft model can guess these tokens most of the time.

To test these assumptions in isolation, we measure the total probability mass “covered” by  $k$  most likely tokens, as well as the probability of top- $k$  tokens guessed by draft models of varying size. If a certain draft model achieves a coverage probability  $p$  for  $k$  tokens, this means that taking the  $k$  most likely tokens predicted by the draft model and measuring their probabilities with the *main* model (Llama-2-Chat 70B) would result in an average cumulative probability equal to  $p$ . We evaluated multiple draft models of various size: JackFram-160M Miao et al. [2023], TinyLlama-1.1B-Chat v1.0 Zhang et al. [2024b], Llama-2-Chat 7B and 13B tou. We report these coverage probabilities on a sample of 512 OpenAssistant conversations Köpf et al. [2023]. For each conversation, we generate 64 additional tokens by sampling from the target 70B model probabilities. We sample these tokens using original probabilities (without temperature or top-p sampling) and use the same tokens for every draft model.

The resulting coverage is reported in Figure 2. This leads to several important observations. First, the target model (Llama-2 Chat 70B) tends to have sharp probability distributions, where the top 1–4 tokens cover 90–98% of the entire probability mass. This agrees with existing observations that language models (esp. the larger ones) are overconfident Miao et al. [2021], Chen et al. [2023b].

Next, we compare how effective the draft models are at predicting these high-probability tokens. While all models eventually get over 90% coverage rate, Llama-2 Chat 7B makes much more accurate predictions with the first 1–4 tokens. This is important for our use case because, while the full draft tree contains thousands of tokens, individual tokens within that tree have much fewer children. Curiously, the 13B draft model demonstrates roughly the same accuracy as 7B despite its larger size.

Though we evaluate coverage for “raw” probabilities from the 70B model, many practical inference scenarios use temperature or nucleus sampling Holtzman et al. [2020]. In fact, the default generation parameters for Llama-2 70B use both a temperature of 0.6 and top-0.9 nucleus sampling Face [2024]. Generating in this way makes the model even more confident, which further improves the efficiency of parallel decoding.

### 5.2 Draft Acceptance Rates

Next, we study how Speculative Execution compares to existing speculative decoding variants for different token budgets. Since all algorithms guarantee that the tokens are sampled from  $P(x_{t+1}|x_{0:t}, \theta_{\text{main}})$ , we compare them in their ability to generate longest sequences of accepted tokens given the same budget of draft tokens.

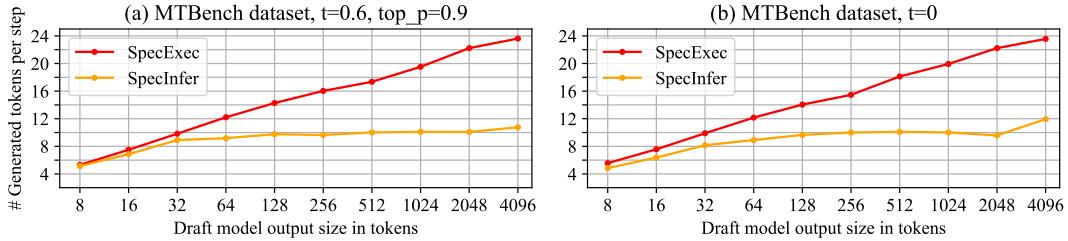


Figure 3: Generation rate depending on the draft budget size for Llama 2-7B Chat as the draft model and Llama 2-70B Chat as the target model, MTBench Zheng et al. [2023] dataset. Results are obtained with an A100 GPU.

Since we are interested in very large budgets, we choose baseline algorithms that better fit this task. The original speculative decoding algorithm Leviathan et al. [2023] generates a single sequence, which is truncated as soon as the algorithm rejects a single token. In other words, using a single long draft sequence results in most of the draft budget being wasted. Therefore, as our baseline, we choose the SpecInfer algorithm that shares the large token budget across multiple stems in a tree.

Similarly to the previous section, we use 70B versions of Llama 2 and Llama 2-Chat as target models. The draft model choice was driven both by the speed and the acceptance rate factors: we found that using draft models with 7B parameters results in significantly more accepted tokens, and a longer forward pass time is still affordable in the offloading setting. We report the effects of these draft models in more detail in Appendix E.

In each setup, we compared SpecExec and SpecInfer, using the 7B draft model, chosen based on our findings from Section 5.1. Figure 3 reports the average number of accepted tokens both for the default sampling configuration (temperature 0.6, top-p 0.9) and for greedy sampling for Llama 2-70B Chat model using the MTBench dataset. Similar tests were run for non-chat models on the C4 dataset; see Figure 4 for results.

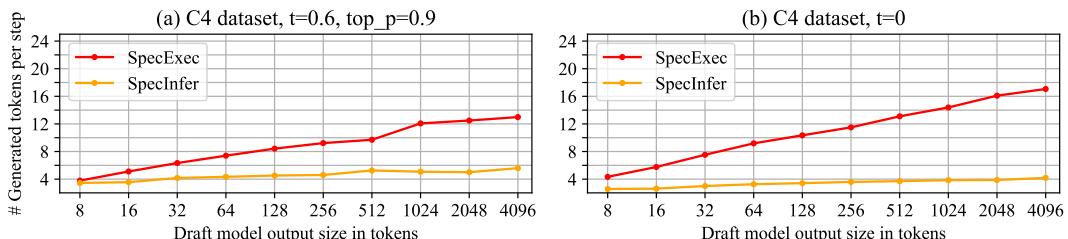


Figure 4: Generation rate depending on the draft budget size for Llama 2-7B Chat as the draft model and Llama 2-70B Chat as the target model, C4 dataset. Results are obtained with an A100 GPU.

For smaller draft budgets, SpecExec performs on par with SpecInfer, but eventually outscals it as we increase the number of draft tokens. We attribute this not to the general verification algorithm, but to the fact that SpecExec constructs its draft out of most likely tokens, while SpecInfer must sample draft tokens to guarantee correctness. We also observe that Speculative Execution achieves a higher margin of improvement on MTBench samples than on C4. It also accepts more tokens with a lower temperature. We attribute this to sharper token probability distributions, leading to higher coverage rates for the same number of draft tokens.

### 5.3 Inference Speed

Finally, we evaluate the practical inference speed of SpecExec by running it with offloading in different hardware configurations. We run these evaluations for Llama 2-70B tou models, both in regular and chat (instruction-tuned) versions. For prompts, we used subsamples of size 100 from OpenAssistant conversations Köpf et al. [2023], WikiText-2 Merity et al. [2016], MTBench Zheng et al. [2023], and C4 Raffel et al. [2020], measuring the speed of generating 32+ tokens per prompt. For Llama 2, we tested two setups: running the main model in 16 bits or quantizing it to 4 bits using GPTQ Frantar et al. [2022]. We also tested Mixtral 8x7B Jiang et al. [2024] (also quantized with GPTQ) and Llama 3 AI [2024] target models in fewer setups.

Table 1: Inference speed with RAM offloading, A100 GPU, Chat / Instruct models, using SpecExec (SX) and SpecInfer (SI) methods. Generation rate (“Gen. rate”) denotes the average number of draft model tokens accepted for one target model iteration.

Draft / Target models	Dataset	t	Method	Budget	Gen. rate	Speed, tok/s	Speedup
Llama 2-7B / 70B	OAsst	0.6	SX	2048	20.60	<b>3.12</b>	<b>18.7x</b>
		0.6	SI	1024	8.41	1.34	8.0x
		0	SX	1024	18.8	<b>2.74</b>	<b>16.4x</b>
		0	SI	1024	7.86	1.18	7.1x
Llama 2-7B / 70B GPTQ	OAsst	0.6	SX	128	12.10	6.02	8.9x
		0	SX	256	13.43	6.17	9.1x
Mistral-7B / Mixtral-8x7B Llama 3-8B / 70B	OAsst	0.6	SX	256	12.38	3.58	3.5x
		0.6	SX	1024	18.88	2.62	15.6x
Llama 3-8B / 70B	MTBench	0.6	SX	1024	18.16	2.79	16.6x
		0	SX	2048	21.58	2.94	17.5x

We measure the inference speed with multiple GPU types: A100 (data-center GPU), RTX 4090 (current generation high-end consumer GPU), RTX 3090 (previous generation consumer GPU), and RTX 2080Ti (older consumer GPU). The first three GPUs are connected to the host via PCIe Gen 4 x16, while 3090 and 2080Ti were tested with PCIe Gen 3 x16. Note that for A100, we report the forward pass time with offloading, even though the GPU can fit a quantized model in its memory. We run all experiments with a batch size of 1 to match the setup of running LLMs on a local machine.

The average inference speed (measured in tokens per second) for A100 GPUs is reported in Tables 1 and 2. While the exact inference speed differs from setup to setup, Speculative Execution consistently speeds up generation with offloading by several times. These results compare favorably with recently published speculative decoding methods using fixed trees like Sequoia Chen et al. [2024b], which attains 2.2 tokens per second in the Llama 3-8B/70B setup, compared to 2.8 tokens per second in case of SpecExec.

In Table 3, we report the results of similar experiments for a range of real-world consumer GPUs. To reduce the memory requirements for the consumer setup, we replaced a 16-bit Llama-2 70B model with a 4-bit GPTQ compressed variant of Llama-2-70B as the target model. To lower the VRAM requirements for 2080 Ti, we used Sheared-Llama-1.3B Xia et al. [2024b] as a draft model, making the whole experiment consume just over 7 GB of VRAM. Note that while the fastest inference time is achieved on RTX 4090, slower consumer GPUs (for example, RTX 2080Ti) still generate tokens quickly enough for interactive use.

Table 2: Inference speed with RAM offloading. A100 GPU, base models, using SpecExec (SX) and SpecInfer (SI). Generation rate (“Gen. rate”) denotes the average number of draft model tokens accepted for one target model iteration.

Draft / Target models	Dataset	t	Method	Budget	Gen. rate	Speed, tok/s	Speedup
Llama 2-7B / 70B	C4	0.6	SX	2048	12.9	<b>1.97</b>	<b>11.8x</b>
		0.6	SI	1024	6.48	1.03	6.2x
		0	SX	2048	16.1	<b>2.38</b>	<b>14.3x</b>
		0	SI	1024	4.78	0.75	4.5x
Llama 2-7B / 70B	WikiText-2	0.6	SX	2048	9.57	<b>1.54</b>	<b>9.2x</b>
		0.6	SI	1024	4.69	0.77	4.6x
		0	SX	2048	11.74	<b>1.88</b>	<b>11.3x</b>
		0	SI	1024	3.71	0.62	3.6x
Llama 2-7B / 70B GPTQ	WikiText-2	0.6	SX	256	6.99	3.72	5.5x
		0	SX	256	8.81	4.54	6.7x
Mistral-7B / Mixtral-8x7B	WikiText-2	0.6	SX	128	6.56	3.23	3.2x

Table 3: SpecExec inference speed on consumer GPUs with offloading, chat/instruct models, Llama 2 70B-GPTQ target model,  $t = 0.6$ , OpenAssistant dataset.

GPU	Draft model	Budget	Gen. rate	Speed, tok/s	Speedup
RTX 4090		256	13.46	5.66	8.3x
RTX 4060	Llama 2-7B	128	9.70	3.28	4.6x
RTX 3090		256	14.3	3.68	10.6x
RTX 2080Ti	ShearedLlama-1.3B	128	7.34	1.86	6.1x

We also explore the relationship between the inference speed and the draft tree size. A larger draft budget allows for a greater number of tokens to be generated per step (see Figure 5 (left)). However, beyond a certain size threshold (hundreds or thousands of tokens, depending on the model and GPU), the time required for generation increases at an accelerating rate (see Figure 1 (right)). Consequently, the optimal draft tree size is typically smaller than the size that maximizes the token acceptance rate. According to our findings, displayed in Figure 5 (right), the optimal draft tree size is 128–512 for SpecInfer and 1024–2048 for SpecExec for the A100 GPU.

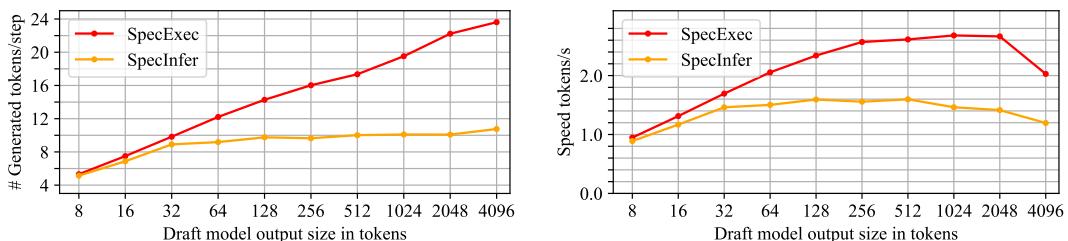


Figure 5: Acceptance counts (left) and generation speed (right) depending on the draft size. Llama 2-7B is used as the draft model, offloaded Llama 2-70B is the target model, MTBench dataset,  $t=0.6$  and top-p=0.9. Results are obtained with an A100 GPU.

While this was not the primary focus area of our study, the SpecExec method can also deliver competitive speedups in inference without offloading; see Appendix G for sample results. Additional tests of SpecExec in generation with penalties show that the method is robust with such conditions: Appendix H provides the results of such an evaluation.

## 6 Conclusion and Future Work

In this work, we propose a method for fast inference of large models on consumer GPUs that unites the efficiency of offloading and speculative decoding in the large-budget setup. The resulting method, SpecExec, shows competitive performance in real-world experimental setups, demonstrating the possibility of running large models locally at the speed of interactive inference.

Although we developed an offloading system to utilize SpecExec in practical settings, the goal of our study was not to create the fastest possible implementation of local LLM inference. Achieving that goal relies on combining our approach with orthogonal performance improvements proposed in prior work, which is beyond the scope of this paper. Importantly, given the recent trends in hardware accelerators for deep learning, inference of large models may become increasingly more constrained by the memory bandwidth even for the fastest devices. Therefore, optimizing generation time with bandwidth constraints in mind is likely to grow more important in the future, and our work demonstrates a novel approach to that problem.

## References

Meta AI. Introducing meta llama 3: The most capable openly available llm to date. <https://ai.meta.com/blog/meta-llama-3/>, 2024.

Joshua Ainslie, James Lee-Thorp, Michiel de Jong, Yury Zemlyanskiy, Federico Lebron, and Sumit Sanghai. GQA: Training generalized multi-query transformer models from multi-head checkpoints. In Houda Bouamor, Juan Pino, and Kalika Bali, editors, *Proceedings of the 2023 Conference on Empirical Methods in Natural Language Processing*, pages 4895–4901, Singapore, December 2023. Association for Computational Linguistics. doi: 10.18653/v1/2023.emnlp-main.298. URL <https://aclanthology.org/2023.emnlp-main.298>.

Keivan Alizadeh, Iman Mirzadeh, Dmitry Belenko, Karen Khatamifar, Minsik Cho, Carlo C Del Mundo, Mohammad Rastegari, and Mehrdad Farajtabar. Llm in a flash: Efficient large language model inference with limited memory. *arXiv preprint arXiv:2312.11514*, 2023.

Reza Yazdani Aminabadi, Samyam Rajbhandari, Ammar Ahmad Awan, Cheng Li, Du Li, Elton Zheng, Olatunji Ruwase, Shaden Smith, Minjia Zhang, Jeff Rasley, and Yuxiong He. Deepspeed-inference: Enabling efficient inference of transformer models at unprecedented scale. In *Proceedings of the International Conference on High Performance Computing, Networking, Storage and Analysis*, SC '22. IEEE Press, 2022. ISBN 9784665454445.

Scott Beamer, Krste Asanović, and David Patterson. The gap benchmark suite. *arXiv preprint arXiv:1508.03619*, 2015.

Maciej Besta, Michał Podstawski, Linus Groner, Edgar Solomonik, and Torsten Hoefler. To push or to pull: On reducing communication and synchronization in graph computations. In *Proceedings of the 26th International Symposium on High-Performance Parallel and Distributed Computing*, pages 93–104, 2017.

Guy E Blelloch, Yan Gu, Yihan Sun, and Kanat Tangwongsan. Parallel shortest paths using radius stepping. In *Proceedings of the 28th ACM Symposium on Parallelism in Algorithms and Architectures*, pages 443–454, 2016.

Nicolas Boulanger-Lewandowski, Yoshua Bengio, and Pascal Vincent. Audio chord recognition with recurrent neural networks. In *ISMIR*, pages 335–340. Curitiba, 2013.

Tianle Cai, Yuhong Li, Zhengyang Geng, Hongwu Peng, and Tri Dao. Medusa: Simple framework for accelerating llm generation with multiple decoding heads. Accessed: 2023-09-08, 2023.

Jerry Chee, Yaohui Cai, Volodymyr Kuleshov, and Christopher De Sa. Quip: 2-bit quantization of large language models with guarantees, 2023.

Charlie Chen, Sébastien Borgeaud, Geoffrey Irving, Jean-Baptiste Lespiau, Laurent Sifre, and John Jumper. Accelerating large language model decoding with speculative sampling. *arXiv preprint arXiv:2302.01318*, 2023a.

Yangyi Chen, Lifan Yuan, Ganqu Cui, Zhiyuan Liu, and Heng Ji. A close look into the calibration of pre-trained language models. In Anna Rogers, Jordan Boyd-Graber, and Naoki Okazaki, editors, *Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pages 1343–1367, Toronto, Canada, July 2023b. Association for Computational Linguistics. doi: 10.18653/v1/2023.acl-long.75. URL <https://aclanthology.org/2023.acl-long.75>.

Zhuoming Chen, Avner May, Ruslan Svirchevski, Yuhsun Huang, Max Ryabinin, Zhihao Jia, and Beidi Chen. Sequoia: Scalable, robust, and hardware-aware speculative decoding, 2024a.

Zhuoming Chen, Avner May, Ruslan Svirchevski, Yuhsun Huang, Max Ryabinin, Zhihao Jia, and Beidi Chen. Sequoia: Sequoia: Serving exact llama2-70b on an rtx4090 with half-second per token latency, 2024b. URL <https://infini-ai-lab.github.io/Sequoia-Page/>. Accessed: 2024-05-21.

Edith Cohen. Using selective path-doubling for parallel shortest-path computations. In *[1993] The 2nd Israel Symposium on Theory and Computing Systems*, pages 78–87. IEEE, 1993.

Edith Cohen. Polylog-time and near-linear work approximation scheme for undirected shortest paths. *Journal of the ACM (JACM)*, 47(1):132–166, 2000.

Andrew Davidson, Sean Baxter, Michael Garland, and John D. Owens. Work-efficient parallel gpu methods for single-source shortest paths. In *2014 IEEE 28th International Parallel and Distributed Processing Symposium*, pages 349–359, 2014. doi: 10.1109/IPDPS.2014.45.

Tim Dettmers. Which gpu(s) to get for deep learning: My experience and advice for using gpus in deep learning, 2023. URL <https://timdettmers.com/2023/01/30/which-gpu-for-deep-learning>. Accessed: 2024-02-29.

Tim Dettmers and Luke Zettlemoyer. The case for 4-bit precision: k-bit inference scaling laws. *arXiv preprint arXiv:2212.09720*, 2022.

Tim Dettmers, Ruslan Svirchevski, Vage Egiazarian, Denis Kuznedelev, Elias Frantar, Saleh Ashkboos, Alexander Borzunov, Torsten Hoefer, and Dan Alistarh. Spqr: A sparse-quantized representation for near-lossless llm weight compression. *arXiv preprint arXiv:2306.03078*, 2023.

Laxman Dhulipala, Guy Blelloch, and Julian Shun. Julienne: A framework for parallel graph algorithms using work-efficient bucketing. In *Proceedings of the 29th ACM Symposium on Parallelism in Algorithms and Architectures*, pages 293–304, 2017.

Edsger W. Dijkstra. A note on two problems in connexion with graphs. *Numerische Mathematik*, 1: 269–271, 1959. URL <https://api.semanticscholar.org/CorpusID:123284777>.

Hugging Face. Meta llama 2-70b chat generation config at hf.co/meta-llama/Llama-2-70b-chat-hf/blob/e1ce257/generation\_config.json, 2024. URL [hf.co/meta-llama/Llama-2-70b-chat-hf/blob/e1ce257/generation\\_config.json](https://hf.co/meta-llama/Llama-2-70b-chat-hf/blob/e1ce257/generation_config.json).

Elias Frantar, Saleh Ashkboos, Torsten Hoefer, and Dan Alistarh. Gptq: Accurate post-training quantization for generative pre-trained transformers. *arXiv preprint arXiv:2210.17323*, 2022.

Yichao Fu, Peter Bailis, Ion Stoica, and Hao Zhang. Break the sequential dependency of llm inference using lookahead decoding. Accessed: 2023-11-29, 2023.

Alex Graves. Sequence transduction with recurrent neural networks. *arXiv preprint arXiv:1211.3711*, 2012.

Yan Gu, Julian Shun, Yihan Sun, and Guy E Blelloch. A top-down parallel semisort. In *Proceedings of the 27th ACM symposium on Parallelism in Algorithms and Architectures*, pages 24–34, 2015.

Pawan Harish and Petter J Narayanan. Accelerating large graph algorithms on the gpu using cuda. In *International conference on high-performance computing*, pages 197–208. Springer, 2007.

Zhenyu He, Zexuan Zhong, Tianle Cai, Jason D Lee, and Di He. Rest: Retrieval-based speculative decoding. *arXiv preprint arXiv:2311.08252*, 2023.

Ari Holtzman, Jan Buys, Li Du, Maxwell Forbes, and Yejin Choi. The curious case of neural text degeneration. In *International Conference on Learning Representations*, 2020. URL <https://openreview.net/forum?id=rygGQyrFvH>.

John Iacono, Ben Karsin, and Nodari Sitchinava. A parallel priority queue with fast updates for GPU architectures. *CoRR*, abs/1908.09378, 2019. URL <http://arxiv.org/abs/1908.09378>.

Albert Q. Jiang, Alexandre Sablayrolles, Arthur Mensch, Chris Bamford, Devendra Singh Chaplot, Diego de las Casas, Florian Bressand, Gianna Lengyel, Guillaume Lample, Lucile Saulnier, Lélio Renard Lavaud, Marie-Anne Lachaux, Pierre Stock, Teven Le Scao, Thibaut Lavril, Thomas Wang, Timothée Lacroix, and William El Sayed. Mistral 7b, 2023.

Albert Q Jiang, Alexandre Sablayrolles, Antoine Roux, Arthur Mensch, Blanche Savary, Chris Bamford, Devendra Singh Chaplot, Diego de las Casas, Emma Bou Hanna, Florian Bressand, et al. Mixtral of experts. *arXiv preprint arXiv:2401.04088*, 2024.

Philip N Klein and Sairam Subramanian. A randomized parallel algorithm for single-source shortest paths. *Journal of Algorithms*, 25(2):205–220, 1997.

Andreas Köpf, Yannic Kilcher, Dimitri von Rütte, Sotiris Anagnostidis, Zhi-Rui Tam, Keith Stevens, Abdullah Barhoum, Nguyen Minh Duc, Oliver Stanley, Richárd Nagyfi, Shahul ES, Sameer Suri, David Glushkov, Arnav Dantuluri, Andrew Maguire, Christoph Schuhmann, Huu Nguyen, and Alexander Mattick. Openassistant conversations – democratizing large language model alignment, 2023.

Butler Lampson. Lazy and speculative execution in computer systems. In Mariam Momenzadeh Alexander A. Shvartsman, editor, *Principles of Distributed Systems*, pages 1–2, Berlin, Heidelberg, 2006. Springer Berlin Heidelberg. ISBN 978-3-540-49991-6.

Yaniv Leviathan, Matan Kalman, and Yossi Matias. Fast inference from transformers via speculative decoding, 2023.

Ji Lin, Jiaming Tang, Haotian Tang, Shang Yang, Xingyu Dang, and Song Han. Awq: Activation-aware weight quantization for llm compression and acceleration. *arXiv preprint arXiv:2306.00978*, 2023.

Xiaoxuan Liu, Lanxiang Hu, Peter Bailis, Ion Stoica, Zhijie Deng, Alvin Cheung, and Hao Zhang. Online speculative decoding. *arXiv preprint arXiv:2310.07177*, 2023.

LocalLlama. Localllama, 2023. URL <https://www.reddit.com/r/LocalLLaMA/>. Accessed: 2023-12-28.

Grzegorz Malewicz, Matthew H Austern, Aart JC Bik, James C Dehnert, Ilan Horn, Naty Leiser, and Grzegorz Czajkowski. Pregel: a system for large-scale graph processing. In *Proceedings of the 2010 ACM SIGMOD International Conference on Management of data*, pages 135–146, 2010.

Stephen Merity, Caiming Xiong, James Bradbury, and Richard Socher. Pointer sentinel mixture models. *arXiv preprint arXiv:1609.07843*, 2016.

Ulrich Meyer. Heaps are better than buckets: parallel shortest paths on unbalanced graphs. In *European Conference on Parallel Processing*, pages 343–351. Springer, 2001.

Mengqi Miao, Fandong Meng, Yijin Liu, Xiao-Hua Zhou, and Jie Zhou. Prevent the language model from being overconfident in neural machine translation. *arXiv preprint arXiv:2105.11098*, 2021.

Xupeng Miao, Gabriele Oliaro, Zhihao Zhang, Xinhao Cheng, Zeyu Wang, Rae Ying Yee Wong, Zhuoming Chen, Daiyaan Arfeen, Reyna Abhyankar, and Zhihao Jia. Specinfer: Accelerating generative llm serving with speculative inference and token tree verification. *arXiv preprint arXiv:2305.09781*, 2023.

Donald Nguyen, Andrew Lenhardt, and Keshav Pingali. A lightweight infrastructure for graph analytics. In *Proceedings of the twenty-fourth ACM symposium on operating systems principles*, pages 456–471, 2013.

Adam Paszke, Sam Gross, Francisco Massa, Adam Lerer, James Bradbury, Gregory Chanan, Trevor Killeen, Zeming Lin, Natalia Gimelshein, Luca Antiga, Alban Desmaison, Andreas Kopf, Edward Yang, Zachary DeVito, Martin Raison, Alykhan Tejani, Sasank Chilamkurthy, Benoit Steiner, Lu Fang, Junjie Bai, and Soumith Chintala. PyTorch: An imperative style, high-performance deep learning library. In *Conference on Neural Information Processing Systems (NeurIPS)*. 2019.

Bharadwaj Pudipeddi, Maral Mesmakhosroshahi, Jinwen Xi, and Sujeeth Bharadwaj. Training large neural networks with constant memory using a new execution algorithm. *CoRR*, abs/2002.05645, 2020. URL <https://arxiv.org/abs/2002.05645>.

Colin Raffel, Noam Shazeer, Adam Roberts, Katherine Lee, Sharan Narang, Michael Matena, Yanqi Zhou, Wei Li, and Peter Liu. Exploring the limits of transfer learning with a unified text-to-text transformer. *Journal of Machine Learning Research*, 21(140):1–67, 2020.

Jie Ren, Samyam Rajbhandari, Reza Yazdani Aminabadi, Olatunji Ruwase, Shuangyan Yang, Minjia Zhang, Dong Li, and Yuxiong He. Zero-offload: Democratizing billion-scale model training. *CoRR*, abs/2101.06840, 2021. URL <https://arxiv.org/abs/2101.06840>.

Ying Sheng, Lianmin Zheng, Binhang Yuan, Zhuohan Li, Max Ryabinin, Beidi Chen, Percy Liang, Christopher Ré, Ion Stoica, and Ce Zhang. Flexgen: High-throughput generative inference of large language models with a single gpu. In *International Conference on Machine Learning*, pages 31094–31116. PMLR, 2023.

Hanmao Shi and Thomas H Spencer. Time–work tradeoffs of the single-source shortest paths problem. *Journal of algorithms*, 30(1):19–32, 1999.

Benjamin Spector and Chris Re. Accelerating llm inference with staged speculative decoding. *arXiv preprint arXiv:2308.04623*, 2023.

Thomas H Spencer. Time-work tradeoffs for parallel algorithms. *Journal of the ACM (JACM)*, 44(5):742–778, 1997.

Mitchell Stern, Noam Shazeer, and Jakob Uszkoreit. Blockwise parallel decoding for deep autoregressive models. *Advances in Neural Information Processing Systems*, 31, 2018.

Ziteng Sun, Ananda Theertha Suresh, Jae Hun Ro, Ahmad Beirami, Himanshu Jain, and Felix Yu. Spectr: Fast speculative decoding via optimal transport. *arXiv preprint arXiv:2310.15141*, 2023.

Ilya Sutskever, Oriol Vinyals, and Quoc V Le. Sequence to sequence learning with neural networks. *Advances in neural information processing systems*, 27, 2014.

Hugo Touvron, Thibaut Lavril, Gautier Izacard, Xavier Martinet, Marie-Anne Lachaux, Timothée Lacroix, Baptiste Rozière, Naman Goyal, Eric Hambro, Faisal Azhar, Aurelien Rodriguez, Armand Joulin, Edouard Grave, and Guillaume Lample. Llama: Open and efficient foundation language models, 2023. URL <https://arxiv.org/abs/2302.13971>.

Albert Tseng, Jerry Chee, Qingyao Sun, Volodymyr Kuleshov, and Christopher De Sa. Quip#: Quip with lattice codebooks, 2023. Accessed: 2024-01-22.

Jeffery Ullman and Mihalis Yannakakis. High-probability parallel transitive closure algorithms. In *Proceedings of the second annual ACM symposium on Parallel algorithms and architectures*, pages 200–209, 1990.

Yangzihao Wang, Andrew Davidson, Yuechao Pan, Yuduo Wu, Andy Riffel, and John D Owens. Gunrock: A high-performance graph processing library on the gpu. In *Proceedings of the 21st ACM SIGPLAN symposium on principles and practice of parallel programming*, pages 1–12, 2016.

Thomas Wolf, Lysandre Debut, Victor Sanh, Julien Chaumond, Clement Delangue, Anthony Moi, Pierrick Cistac, Tim Rault, Rémi Louf, Morgan Funtowicz, et al. Huggingface’s transformers: State-of-the-art natural language processing. *arXiv preprint arXiv:1910.03771*, 2019.

Heming Xia, Zhe Yang, Qingxiu Dong, Peiyi Wang, Yongqi Li, Tao Ge, Tianyu Liu, Wenjie Li, and Zhifang Sui. Unlocking efficiency in large language model inference: A comprehensive survey of speculative decoding, 2024a. URL <https://arxiv.org/abs/2401.07851>.

Mengzhou Xia, Tianyu Gao, Zhiyuan Zeng, and Danqi Chen. Sheared llama: Accelerating language model pre-training via structured pruning, 2024b.

Daliang Xu, Wangsong Yin, Xin Jin, Ying Zhang, Shiyun Wei, Mengwei Xu, and Xuanzhe Liu. Llm-cad: Fast and scalable on-device large language model inference. *arXiv preprint arXiv:2309.04255*, 2023.

Chen Zhang, Zhuorui Liu, and Dawei Song. Beyond the speculative game: A survey of speculative execution in large language models, 2024a. URL <https://arxiv.org/abs/2404.14897>.

Jun Zhang, Jue Wang, Huan Li, Lidan Shou, Ke Chen, Gang Chen, and Sharad Mehrotra. Draft & verify: Lossless large language model acceleration via self-speculative decoding. *arXiv preprint arXiv:2309.08168*, 2023.

Peiyuan Zhang, Guangtao Zeng, Tianduo Wang, and Wei Lu. Tinyllama: An open-source small language model, 2024b.

Yunming Zhang, Ajay Brahmakshatriya, Xinyi Chen, Laxman Dhulipala, Shoaib Kamil, Saman Amarasinghe, and Julian Shun. Optimizing ordered graph algorithms with graphit. In *Proceedings of the 18th ACM/IEEE International Symposium on Code Generation and Optimization*, pages 158–170, 2020.

Lianmin Zheng, Wei-Lin Chiang, Ying Sheng, Siyuan Zhuang, Zhanghao Wu, Yonghao Zhuang, Zi Lin, Zhuohan Li, Dacheng Li, Eric. P Xing, Hao Zhang, Joseph E. Gonzalez, and Ion Stoica. Judging llm-as-a-judge with mt-bench and chatbot arena, 2023.

Xiaowei Zhu, Wenguang Chen, Weimin Zheng, and Xiaosong Ma. Gemini: A {Computation-Centric} distributed graph processing system. In *12th USENIX Symposium on Operating Systems Design and Implementation (OSDI 16)*, pages 301–316, 2016.

## A Equivalence of Optimal Tree Search to Shortest Path Search

We can formulate this problem as follows:

$$\arg \max_{\tau \in \mathcal{T}^K} \sum_{x_i \in \tau} P_{\text{reach}}(x_i | \tau) \cdot P_{\text{accept}}(x_i | \tau). \quad (1)$$

Here,  $x_i \in \tau$  refers to a token within the draft tree,  $\mathcal{T}^K$  is a set of all trees of  $K$  tokens and  $P_{\text{reach}}(x_i | \tau)$  is the probability that the Speculative Execution verification phase accepts the full prefix  $x_0, \dots, x_{i-1}$  along the draft tree and considers sampling  $x_i$  next. Finally,  $P_{\text{accept}}(x_i | \tau)$  is the probability that the token  $x_i$  will be accepted *if* it is reached during verification. Both  $P_{\text{reach}}$  and  $P_{\text{accept}}$  depend on the target model probabilities  $P(x_{t+1} | x_{0:t}, \theta_{\text{target}})$ , which cannot be accessed in the drafting phase. Instead, we use the draft model to approximate the target model probabilities as follows:

$$\begin{aligned} P_{\text{reach}}(x_i | \tau) &\approx \prod_{x_t \in \pi(x_i, \tau)} P(x_t | \pi(x_t, \tau), \theta_{\text{draft}}) \\ P_{\text{accept}}(x_i | \tau) &\approx P(x_i | \pi(x_i, \tau), \theta_{\text{draft}}), \end{aligned} \quad (2)$$

where  $\pi(x_i, \tau)$  is the path in  $\tau$  from root to  $x_i$ , excluding  $x_i$  itself. From the LLM perspective,  $\pi(x_i, \tau)$  is the prefix for a token  $x_i$  within the draft tree. If we multiply the two expressions as per Equation 1, we get the cumulative probability of a sequence  $\pi(x_i, \tau) \oplus x_i$ , where  $\oplus$  is concatenation.

$$\arg \max_{\tau \in \mathcal{T}^K} \sum_{x_i \in \tau} \prod_{x_t \in \pi(x_i, \tau) \oplus x_i} P(x_t | \pi(x_t, \tau), \theta_{\text{draft}}) \quad (3)$$

Since token probabilities cannot be greater than 1, the cumulative probability of  $\pi(x_i, \tau) \oplus x_i$  cannot exceed the cumulative probability of all tokens in  $\pi(x_i, \tau)$ . Therefore, if a token  $x_i$  is among the  $K$  most likely tokens, every token in  $\pi(x_i, \tau)$  is also a part of the solution. Using this property, we can simplify Equation 3 as finding top- $K$  most likely prefixes, since they are guaranteed to form a tree. Formally speaking, the optimal tree consists of  $K$  tokens with the highest cumulative probability:

$$\arg \max_{x_i} \prod_{x_t \in \pi(x_i, \tau) \oplus x_i} P(x_t | \pi(x_t, \tau), \theta_{\text{draft}}) \quad (4)$$

This is similar (but not equivalent) to the standard beam search algorithm for neural sequence models Graves [2012], Boulanger-Lewandowski et al. [2013], Sutskever et al. [2014]. The main difference is that beam search looks for complete sequences, while we need a tree of partial drafts. However, using beam search instead of solving Equation 3 directly leads to suboptimal drafts (see Appendix F for details).

Instead, we solve Equation 4 by reformulating it as a special case of the shortest path search problem. More specifically,

$$\begin{aligned} \arg \max_{x_i} \prod_{x_t \in \pi(x_i, \tau) \oplus x_i} P(x_t | \pi(x_t, \tau), \theta_{\text{draft}}) &= \\ = \arg \max_{x_i} \sum_{x_t \in \pi(x_i, \tau) \oplus x_i} \log P(x_t | \pi(x_t, \tau), \theta_{\text{draft}}) &= \\ = \arg \min_{x_i} \sum_{x_t \in \pi(x_i, \tau) \oplus x_i} -\log P(x_t | \pi(x_t, \tau), \theta_{\text{draft}}). & \end{aligned} \quad (5)$$

Note that every term in that sum is non-negative, (since  $-\log P(x_t | \pi(x_t, \tau), \theta_{\text{draft}}) \geq 0$ ), which makes this equivalent to a single-source shortest path (SSSP) problem for finding paths to  $K$  nearest nodes in a graph with non-negative edge weights. Normally, this problem can be solved by running the Dijkstra algorithm for  $K$  steps. However, in practice, running the algorithm for  $K$  sequential steps is inefficient on modern highly parallel hardware, especially in our setting with very large drafts. To alleviate this problem, we use a modified parallel Dijkstra algorithm, which expands  $B > 1$  nodes on every iteration and keeps track of  $K$  nearest nodes in a priority queue. We describe this formally in Algorithm 2.

In the worst case, this algorithm still makes up to  $K$  steps if the solution to Equation 3 is a single “stem”  $B$  tokens long. However, the actual number of steps is significantly lower, often slightly above the lower bound  $\lceil B/K \rceil$ . In the practical GPU implementation, we also limit the maximum depth with a parameter  $D$ . The purpose of  $D$  is to limit the edge case where the draft model is very confident about the next token, and thus the solution to Equation 3 is a single sequence of length  $K$ . For this edge case, Algorithm 2 will take long to generate a sequential draft, most of which will later be discarded if the draft model makes even one mistake.

## B SpecExec Algorithm Diagram

Figure 6 displays a block diagram that outlines the key steps of the SpecExec algorithm.

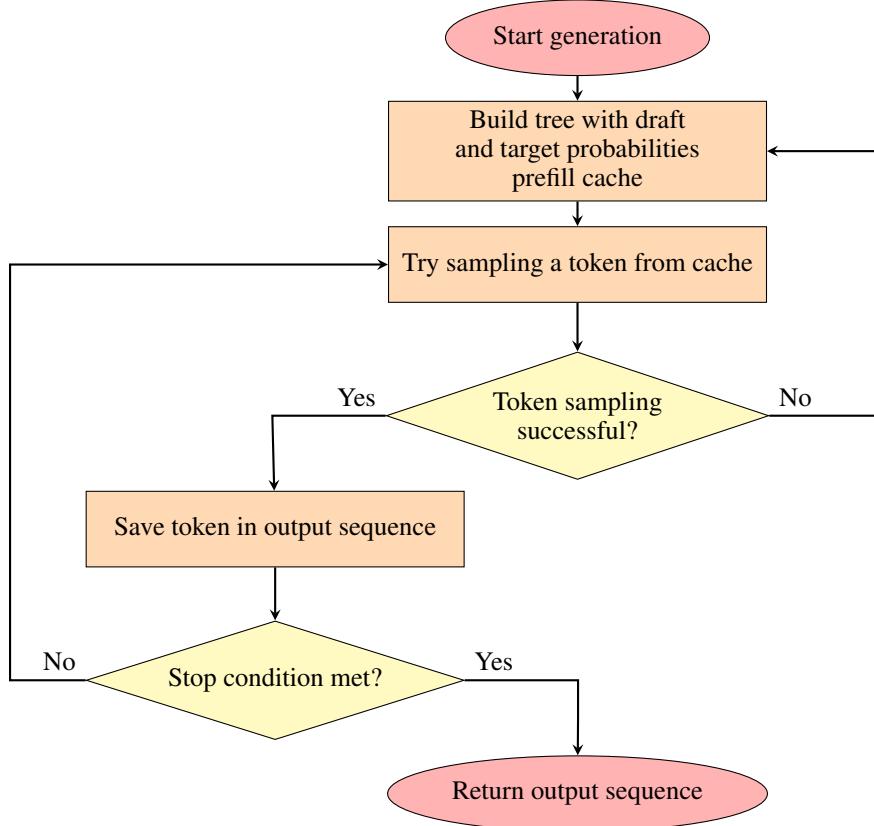


Figure 6: A high-level overview of the SpecExec algorithm.

## C Parallel Graph Search

There are dozens of works that study practical implementations of parallel shortest path search and SSSP in particular. One line of work proposes inexact search algorithms that use an approximate priority queue to improve the performance of SSSP: Nguyen et al. [2013] proposes a queue with an integer metric, and Zhang et al. [2020] adds bucket fusion to reduce the synchronization overhead..

A significant effort was dedicated to efficient shortest-path search on GPUs, among others. Harish and Narayanan [2007] proposes a GPU-efficient SSSP that outperforms sequential CPU computations. Davidson et al. [2014], Wang et al. [2016] compare several SSSP variants for GPUs. Iacono et al. [2019] adapts priority queues to run efficiently on GPU and uses the resulting data structure to accelerate SSSP.

Many works on parallel graph search focus on the distributed setting Malewicz et al. [2010], Zhu et al. [2016], Besta et al. [2017], addressing communication and synchronization overheads. Finally,

a large body of work studies the theoretical properties of parallel SSSP, including Ullman and Yannakakis [1990], Klein and Subramanian [1997], Cohen [1993], Shi and Spencer [1999], Cohen [2000], Spencer [1997], Meyer [2001], Blelloch et al. [2016].

## D Additional Implementation Details

Our system design follows the following loop:

1. Load the draft model onto GPU memory and generate a draft tree;
2. Load the main model (several layers at a time, if using offloading) to compute probabilities for the draft tree tokens;
3. Choose the accepted tokens following the verification procedure.

When running the main model, we process all draft tokens in parallel by constructing a merged attention mask, similar to Miao et al. [2023]. We prefetch the first few layers of the main model during speculation to speed up the procedure. We also load subsequent LLM layers in parallel, while the previous layers compute their activations, as described in Pudipeddi et al. [2020], Aminabadi et al. [2022].

Finally, we keep the past key/value caches of both draft and main models in GPU memory at all times. We chose this because most modern language models use grouped-query attention Ainslie et al. [2023], making caches relatively small for short prompts. When dealing with longer prompts or smaller GPU memory, one can reduce memory usage by offloading these KV caches into RAM. The draft model caches are only needed on GPU during the first stage when generating the draft tokens. In turn, the main model caches can be loaded alongside their transformer layers.

The optimal implementation of this algorithm is slightly different depending on the hardware configuration. Running SpecExec on a system with GPU with RAM offloading works best with relatively fewer draft tokens, while longer offloading (to SSD or when using float16 precision weights) works best with larger token budgets.

As for the quantization scheme, while there are better quantization algorithms Lin et al. [2023], Dettmers et al. [2023], Chee et al. [2023], we chose GPTQ since it is popular among practitioners. Still, we believe that our experimental results will generalize to other quantization algorithms. In addition to the main model, we also quantize the draft (7B) model using the same GPTQ algorithm. The optimal choices of the quantization methods will vary as new methods or faster implementations appear.

The experiments were mainly performed using A100 GPUs (unless specified otherwise), but may be easily reproduced using other GPUs. Note that while A100 has 80GB VRAM, we did not keep any layers in VRAM in order to keep the VRAM use to minimum and emulate performance of GPUs like RTX4090 or L40. As a result, the observed VRAM use requirements with offloading was in 12–22 GB range for experiments with draft trees up to 2048 tokens when using Llama-2-70B RAM offloading. Naturally, keeping some of the layers constantly in VRAM would increase both baseline and the model performance.

The offloading experiments require sufficient RAM to hold whole model. In case of Llama-2-70B in 16 bit, this is at least 140 GB, but in practice 192 GB would be recommended to fit the draft model, caches and memory of other processes. Our code is based on industry standard PyTorch Paszke et al. [2019] and Transformers Wolf et al. [2019] libraries.

## E Ablation: Acceptance with Different Draft Models

In Section 5.2, we evaluate SpecExec and SpecInfer with 7B draft models based on the observations about their coverage probabilities. Here, we further compare these models in terms of the number of accepted tokens for different SpecExec batch sizes. We report the results of this comparison in Figure 7 using the same OpenAssistant dataset as in the main experiments using the recommended temperature (0.6) and nucleus size (0.9). Similarly to Figure 2, the 7B model significantly outperforms both JackFram/llama-160m and TinyLlama 1.1B Chat. This is true both for the original 7B model and the one quantized to 4 bits with GPTQ. Curiously, the full unquantized 13B model still obtains

slightly more accepted tokens, though at the cost of 26GB memory footprint that is inaccessible to modern consumer GPUs.

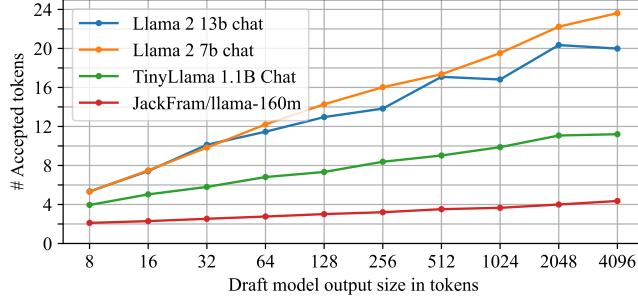


Figure 7: Number of accepted tokens as a function of the draft size  $B$  for the Llama 2-70B Chat target model and different draft models.

## F On The Suboptimality of Beam Search

In our preliminary experiments, we tried to construct the optimal draft tree using top-k beam search decoding Graves [2012]. However, we observed that the algorithm performed significantly worse than expected and often plateaued as we increased the maximum beam search length. Here, we describe the analysis of this problem that eventually led us to Algorithm 2.

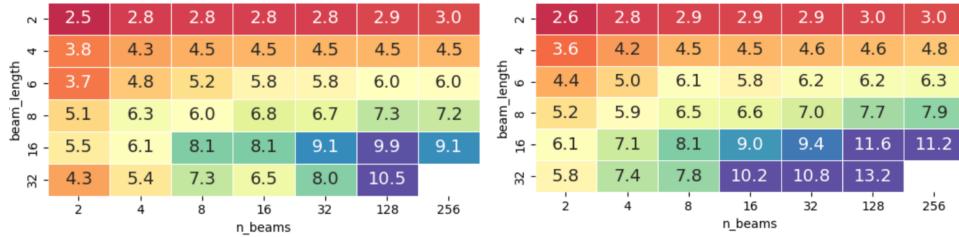


Figure 8: The average number of accepted tokens per speculation and verification phases as a function of beam size and maximum length. The measurements are obtained on OpenAssistant conversations (Left) and WikiText-2 articles (Right) for running with recommended generation parameters (temperature 0.6, top-p 0.9). **(Left)** standard beam search decoding, **(Right)** beam search without pruning out-of-beam tokens.

Figure 8 (left) reports a grid where each cell is the number of accepted tokens for a version of SpecExec that uses beam search instead of parallel SSSP. The horizontal grid axis corresponds to beam size (also known as the number of beams), and the vertical axis depicts maximum length within a beam. The left grid shows standard beam search decoding that returns beam size most likely sequences. In turn, the right grid uses a modified search algorithm that starts the same way as beam search but does not prune any partial hypotheses that did not make it into the final beam.

As we can see, standard beam search decoding is suboptimal for SpecExec in the sense that it can be outperformed with trivial modifications. In turn, Algorithm 2 is a generalization of the version on the right that does not need to be manually tuned for length and width, but instead expands the graph optimally to maximize the coverage probability.

## G Application to in-memory inference

While this was not the primary focus area of our research, the SpecExec method can also deliver measurable speedups in inference without offloading. While these speedups are less impressive than those for offload settings, they are still competitive when compared to recent works such as Chen et al. [2024a].

Table 4: SpecExec Inference speed without offloading, A100 GPU.

Draft / Target models	Dataset	t	Method	Budget	Gen. rate	Speed, tok/s	Speedup
SL-1.3B / Vicuna-33B	OASST-1	0.6	SX	128	5.33	31.6	2.15x
	OASST-1	0	SX	128	5.4	32.94	2.24x
	C4	0.6	SX	128	5.1	33.3	2.26x
		0	SX	128	5.36	35.62	2.42x
	WikiText-2	0.6	SX	128	4.87	30.19	1.90x
	WikiText-2	0	SX	128	5.24	33.15	2.08x

## H Drafting penalty effects

To verify the method’s robustness, we ran a series of experiments with penalties excluding the use of specific tokens. The same penalty scheme was applied to both draft and target models, and the expectation is that the models should be able to run SpecExec effectively. To verify this claim, we ran a series of experiments with penalties excluding use of fewer or more tokens. For these experiments, we penalized all tokens that start from the letter “r” (left) or all tokens that contain the letter “r” (right). Here we used the Llama 2-7B Chat target model with TinyLlama-1.1B Chat draft model, t=0.6, p=0.9, MT-Bench dataset.

The results of these experiments can be found in Figure 9. We found that our method’s performance (measured in terms of accepted tokens per iteration) stays stable only with lightweight penalties, yet heavier penalties reduce the absolute speedups. Looking at the generated samples, we observed that while with lighter penalties, the model is able to work around the restrictions and generate reasonable text, with heavier penalties the quality deteriorated as the model skipped or replaced tokens seemingly at random. Stronger penalties affect the quality of the generated text and naturally make the task harder for the draft model. Thus, we attribute the lower performance with a heavy penalty to this perplexity increase rather than to the penalty directly.

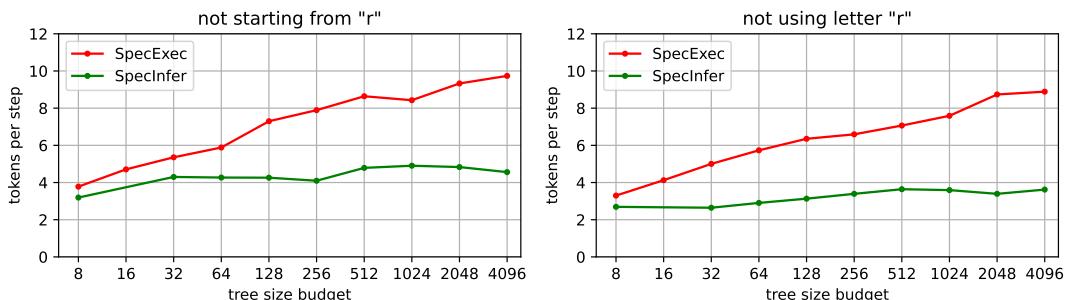


Figure 9: Acceptance rate in generation with token penalty: “don’t start words with “R”” (left) and “don’t use the letter “R”” (right); Llama 2 7B Chat (+ TinyLlama-1.1B Chat draft) model (t=0.6, p=0.9), MT-Bench dataset. The rest of the experimental configuration is the same as in Figure 1.

## NeurIPS Paper Checklist

### 1. Claims

Question: Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope?

Answer: **[Yes]**

Justification: The abstract and introduction contain the summary of our results, specifically the achieved speedups.

Guidelines:

- The answer NA means that the abstract and introduction do not include the claims made in the paper.
- The abstract and/or introduction should clearly state the claims made, including the contributions made in the paper and important assumptions and limitations. A No or NA answer to this question will not be perceived well by the reviewers.
- The claims made should match theoretical and experimental results, and reflect how much the results can be expected to generalize to other settings.
- It is fine to include aspirational goals as motivation as long as it is clear that these goals are not attained by the paper.

### 2. Limitations

Question: Does the paper discuss the limitations of the work performed by the authors?

Answer: **[Yes]**

Justification: The proposed algorithm performs best when the drafting model is of high quality and well aligned with the target model. This may become a practical obstacle in obtaining high throughput in settings with comparatively low inference cycle time of the target model, namely without offloading. Additionally, the method is performing less impressively when used with quantized models since those start requiring significantly greater run time with moderate-to high batch sizes.

Guidelines:

- The answer NA means that the paper has no limitation while the answer No means that the paper has limitations, but those are not discussed in the paper.
- The authors are encouraged to create a separate "Limitations" section in their paper.
- The paper should point out any strong assumptions and how robust the results are to violations of these assumptions (e.g., independence assumptions, noiseless settings, model well-specification, asymptotic approximations only holding locally). The authors should reflect on how these assumptions might be violated in practice and what the implications would be.
- The authors should reflect on the scope of the claims made, e.g., if the approach was only tested on a few datasets or with a few runs. In general, empirical results often depend on implicit assumptions, which should be articulated.
- The authors should reflect on the factors that influence the performance of the approach. For example, a facial recognition algorithm may perform poorly when image resolution is low or images are taken in low lighting. Or a speech-to-text system might not be used reliably to provide closed captions for online lectures because it fails to handle technical jargon.
- The authors should discuss the computational efficiency of the proposed algorithms and how they scale with dataset size.
- If applicable, the authors should discuss possible limitations of their approach to address problems of privacy and fairness.
- While the authors might fear that complete honesty about limitations might be used by reviewers as grounds for rejection, a worse outcome might be that reviewers discover limitations that aren't acknowledged in the paper. The authors should use their best judgment and recognize that individual actions in favor of transparency play an important role in developing norms that preserve the integrity of the community. Reviewers will be specifically instructed to not penalize honesty concerning limitations.

### 3. Theory Assumptions and Proofs

Question: For each theoretical result, does the paper provide the full set of assumptions and a complete (and correct) proof?

Answer: [Yes]

Justification: In this paper's theoretical analysis, we mostly refer to the results proven earlier, however for the equivalence of optimal tree search to shortest path search, we provide a proof in the appendix.

Guidelines:

- The answer NA means that the paper does not include theoretical results.
- All the theorems, formulas, and proofs in the paper should be numbered and cross-referenced.
- All assumptions should be clearly stated or referenced in the statement of any theorems.
- The proofs can either appear in the main paper or the supplemental material, but if they appear in the supplemental material, the authors are encouraged to provide a short proof sketch to provide intuition.
- Inversely, any informal proof provided in the core of the paper should be complemented by formal proofs provided in appendix or supplemental material.
- Theorems and Lemmas that the proof relies upon should be properly referenced.

### 4. Experimental Result Reproducibility

Question: Does the paper fully disclose all the information needed to reproduce the main experimental results of the paper to the extent that it affects the main claims and/or conclusions of the paper (regardless of whether the code and data are provided or not)?

Answer: [Yes]

Justification: Our results are reproducible using the attached code. The necessary setup details are given in the manuscript of the paper and in the appendix named "Additional Implementation Details".

Guidelines:

- The answer NA means that the paper does not include experiments.
- If the paper includes experiments, a No answer to this question will not be perceived well by the reviewers: Making the paper reproducible is important, regardless of whether the code and data are provided or not.
- If the contribution is a dataset and/or model, the authors should describe the steps taken to make their results reproducible or verifiable.
- Depending on the contribution, reproducibility can be accomplished in various ways. For example, if the contribution is a novel architecture, describing the architecture fully might suffice, or if the contribution is a specific model and empirical evaluation, it may be necessary to either make it possible for others to replicate the model with the same dataset, or provide access to the model. In general, releasing code and data is often one good way to accomplish this, but reproducibility can also be provided via detailed instructions for how to replicate the results, access to a hosted model (e.g., in the case of a large language model), releasing of a model checkpoint, or other means that are appropriate to the research performed.
- While NeurIPS does not require releasing code, the conference does require all submissions to provide some reasonable avenue for reproducibility, which may depend on the nature of the contribution. For example
  - (a) If the contribution is primarily a new algorithm, the paper should make it clear how to reproduce that algorithm.
  - (b) If the contribution is primarily a new model architecture, the paper should describe the architecture clearly and fully.
  - (c) If the contribution is a new model (e.g., a large language model), then there should either be a way to access this model for reproducing the results or a way to reproduce the model (e.g., with an open-source dataset or instructions for how to construct the dataset).

(d) We recognize that reproducibility may be tricky in some cases, in which case authors are welcome to describe the particular way they provide for reproducibility. In the case of closed-source models, it may be that access to the model is limited in some way (e.g., to registered users), but it should be possible for other researchers to have some path to reproducing or verifying the results.

## 5. Open access to data and code

Question: Does the paper provide open access to the data and code, with sufficient instructions to faithfully reproduce the main experimental results, as described in supplemental material?

Answer: **[Yes]**

Justification: The experiments for this paper only use openly available datasets and code libraries. The code with launch instructions is attached to the paper submission and we intend to keep it open.

Guidelines:

- The answer NA means that paper does not include experiments requiring code.
- Please see the NeurIPS code and data submission guidelines (<https://nips.cc/public/guides/CodeSubmissionPolicy>) for more details.
- While we encourage the release of code and data, we understand that this might not be possible, so “No” is an acceptable answer. Papers cannot be rejected simply for not including code, unless this is central to the contribution (e.g., for a new open-source benchmark).
- The instructions should contain the exact command and environment needed to run to reproduce the results. See the NeurIPS code and data submission guidelines (<https://nips.cc/public/guides/CodeSubmissionPolicy>) for more details.
- The authors should provide instructions on data access and preparation, including how to access the raw data, preprocessed data, intermediate data, and generated data, etc.
- The authors should provide scripts to reproduce all experimental results for the new proposed method and baselines. If only a subset of experiments are reproducible, they should state which ones are omitted from the script and why.
- At submission time, to preserve anonymity, the authors should release anonymized versions (if applicable).
- Providing as much information as possible in supplemental material (appended to the paper) is recommended, but including URLs to data and code is permitted.

## 6. Experimental Setting/Details

Question: Does the paper specify all the training and test details (e.g., data splits, hyper-parameters, how they were chosen, type of optimizer, etc.) necessary to understand the results?

Answer: **[Yes]**

Justification: The paper, together with the “Additional Implementation Details” appendix and instructions in the code, contain information on all substantial details necessary to understand the results.

Guidelines:

- The answer NA means that the paper does not include experiments.
- The experimental setting should be presented in the core of the paper to a level of detail that is necessary to appreciate the results and make sense of them.
- The full details can be provided either with the code, in appendix, or as supplemental material.

## 7. Experiment Statistical Significance

Question: Does the paper report error bars suitably and correctly defined or other appropriate information about the statistical significance of the experiments?

Answer: **[No]**

Justification: Following the setting of the past papers in the speculative decoding area, we focus on providing the attained generation speed and acceptance rates.

Guidelines:

- The answer NA means that the paper does not include experiments.
- The authors should answer "Yes" if the results are accompanied by error bars, confidence intervals, or statistical significance tests, at least for the experiments that support the main claims of the paper.
- The factors of variability that the error bars are capturing should be clearly stated (for example, train/test split, initialization, random drawing of some parameter, or overall run with given experimental conditions).
- The method for calculating the error bars should be explained (closed form formula, call to a library function, bootstrap, etc.)
- The assumptions made should be given (e.g., Normally distributed errors).
- It should be clear whether the error bar is the standard deviation or the standard error of the mean.
- It is OK to report 1-sigma error bars, but one should state it. The authors should preferably report a 2-sigma error bar than state that they have a 96% CI, if the hypothesis of Normality of errors is not verified.
- For asymmetric distributions, the authors should be careful not to show in tables or figures symmetric error bars that would yield results that are out of range (e.g. negative error rates).
- If error bars are reported in tables or plots, The authors should explain in the text how they were calculated and reference the corresponding figures or tables in the text.

## 8. Experiments Compute Resources

Question: For each experiment, does the paper provide sufficient information on the computer resources (type of compute workers, memory, time of execution) needed to reproduce the experiments?

Answer: [\[Yes\]](#)

Justification: In the paper and in the "Additional Implementation Details" appendix, we list the GPU types used and indicative memory requirements.

Guidelines:

- The answer NA means that the paper does not include experiments.
- The paper should indicate the type of compute workers CPU or GPU, internal cluster, or cloud provider, including relevant memory and storage.
- The paper should provide the amount of compute required for each of the individual experimental runs as well as estimate the total compute.
- The paper should disclose whether the full research project required more compute than the experiments reported in the paper (e.g., preliminary or failed experiments that didn't make it into the paper).

## 9. Code Of Ethics

Question: Does the research conducted in the paper conform, in every respect, with the NeurIPS Code of Ethics <https://neurips.cc/public/EthicsGuidelines>?

Answer: [\[Yes\]](#)

Justification: Yes, we confirm adherence to the NeurIPS Code of Ethics.

Guidelines:

- The answer NA means that the authors have not reviewed the NeurIPS Code of Ethics.
- If the authors answer No, they should explain the special circumstances that require a deviation from the Code of Ethics.
- The authors should make sure to preserve anonymity (e.g., if there is a special consideration due to laws or regulations in their jurisdiction).

## 10. Broader Impacts

Question: Does the paper discuss both potential positive societal impacts and negative societal impacts of the work performed?

Answer: [NA]

Justification: This paper studies the efficient inference of large language models on accelerators with limited memory. Importantly, using LLMs in these environments is already possible due to a considerable number of previously proposed algorithms, as the research area is well-known within the machine learning community. The method we propose does not affect the task performance of the language model it is applied to, as it only improves the speed of generation with that model. Therefore, we feel that no potential consequences of LLM use (aside from those already discussed in past work) need to be specifically highlighted in our paper.

Guidelines:

- The answer NA means that there is no societal impact of the work performed.
- If the authors answer NA or No, they should explain why their work has no societal impact or why the paper does not address societal impact.
- Examples of negative societal impacts include potential malicious or unintended uses (e.g., disinformation, generating fake profiles, surveillance), fairness considerations (e.g., deployment of technologies that could make decisions that unfairly impact specific groups), privacy considerations, and security considerations.
- The conference expects that many papers will be foundational research and not tied to particular applications, let alone deployments. However, if there is a direct path to any negative applications, the authors should point it out. For example, it is legitimate to point out that an improvement in the quality of generative models could be used to generate deepfakes for disinformation. On the other hand, it is not needed to point out that a generic algorithm for optimizing neural networks could enable people to train models that generate Deepfakes faster.
- The authors should consider possible harms that could arise when the technology is being used as intended and functioning correctly, harms that could arise when the technology is being used as intended but gives incorrect results, and harms following from (intentional or unintentional) misuse of the technology.
- If there are negative societal impacts, the authors could also discuss possible mitigation strategies (e.g., gated release of models, providing defenses in addition to attacks, mechanisms for monitoring misuse, mechanisms to monitor how a system learns from feedback over time, improving the efficiency and accessibility of ML).

## 11. Safeguards

Question: Does the paper describe safeguards that have been put in place for responsible release of data or models that have a high risk for misuse (e.g., pretrained language models, image generators, or scraped datasets)?

Answer: [NA]

Justification: This paper does not alter the capabilities of the available models or datasets, but rather provides a more efficient approach to use them on hardware with limited capabilities. Thus, we believe that our paper has a neutral risk impact in this area.

Guidelines:

- The answer NA means that the paper poses no such risks.
- Released models that have a high risk for misuse or dual-use should be released with necessary safeguards to allow for controlled use of the model, for example by requiring that users adhere to usage guidelines or restrictions to access the model or implementing safety filters.
- Datasets that have been scraped from the Internet could pose safety risks. The authors should describe how they avoided releasing unsafe images.
- We recognize that providing effective safeguards is challenging, and many papers do not require this, but we encourage authors to take this into account and make a best faith effort.

## 12. Licenses for existing assets

Question: Are the creators or original owners of assets (e.g., code, data, models), used in the paper, properly credited and are the license and terms of use explicitly mentioned and properly respected?

Answer: [\[Yes\]](#)

Justification: We included references to the models, datasets, and other assets used in this paper. We believe that our use of these assets is consistent with their respective license terms.

Guidelines:

- The answer NA means that the paper does not use existing assets.
- The authors should cite the original paper that produced the code package or dataset.
- The authors should state which version of the asset is used and, if possible, include a URL.
- The name of the license (e.g., CC-BY 4.0) should be included for each asset.
- For scraped data from a particular source (e.g., website), the copyright and terms of service of that source should be provided.
- If assets are released, the license, copyright information, and terms of use in the package should be provided. For popular datasets, [paperswithcode.com/datasets](http://paperswithcode.com/datasets) has curated licenses for some datasets. Their licensing guide can help determine the license of a dataset.
- For existing datasets that are re-packaged, both the original license and the license of the derived asset (if it has changed) should be provided.
- If this information is not available online, the authors are encouraged to reach out to the asset's creators.

### 13. New Assets

Question: Are new assets introduced in the paper well documented and is the documentation provided alongside the assets?

Answer: [\[Yes\]](#)

Justification: We made an effort to document the proposed method and added its code implementation with appropriate instructions.

Guidelines:

- The answer NA means that the paper does not release new assets.
- Researchers should communicate the details of the dataset/code/model as part of their submissions via structured templates. This includes details about training, license, limitations, etc.
- The paper should discuss whether and how consent was obtained from people whose asset is used.
- At submission time, remember to anonymize your assets (if applicable). You can either create an anonymized URL or include an anonymized zip file.

### 14. Crowdsourcing and Research with Human Subjects

Question: For crowdsourcing experiments and research with human subjects, does the paper include the full text of instructions given to participants and screenshots, if applicable, as well as details about compensation (if any)?

Answer: [\[NA\]](#)

Justification: The experiments in the paper did not require crowdsourcing or human subjects.

Guidelines:

- The answer NA means that the paper does not involve crowdsourcing nor research with human subjects.
- Including this information in the supplemental material is fine, but if the main contribution of the paper involves human subjects, then as much detail as possible should be included in the main paper.

- According to the NeurIPS Code of Ethics, workers involved in data collection, curation, or other labor should be paid at least the minimum wage in the country of the data collector.

#### **15. Institutional Review Board (IRB) Approvals or Equivalent for Research with Human Subjects**

Question: Does the paper describe potential risks incurred by study participants, whether such risks were disclosed to the subjects, and whether Institutional Review Board (IRB) approvals (or an equivalent approval/review based on the requirements of your country or institution) were obtained?

Answer: [NA]

Justification: The experiments in the paper did not require crowdsourcing or human subjects.

Guidelines:

- The answer NA means that the paper does not involve crowdsourcing nor research with human subjects.
- Depending on the country in which research is conducted, IRB approval (or equivalent) may be required for any human subjects research. If you obtained IRB approval, you should clearly state this in the paper.
- We recognize that the procedures for this may vary significantly between institutions and locations, and we expect authors to adhere to the NeurIPS Code of Ethics and the guidelines for their institution.
- For initial submissions, do not include any information that would break anonymity (if applicable), such as the institution conducting the review.