

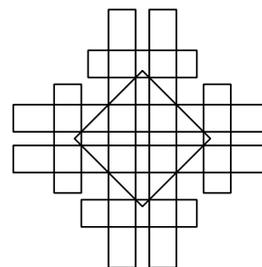
# 41st International Symposium on Computational Geometry

SoCG 2025, June 23–27, 2025, Kanazawa, Japan

Edited by

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PART 1



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*ACM Classification 2012*

Theory of computation → Computational geometry; Theory of computation → Design and analysis of algorithms; Mathematics of computing → Combinatorics; Mathematics of computing → Graph algorithms

**ISBN 978-3-95977-370-6**

**PRINT ISBN 979-8-3313-2287-8**

*Published online and open access by*

Schloss Dagstuhl – Leibniz-Zentrum für Informatik GmbH, Dagstuhl Publishing, Saarbrücken/Wadern, Germany. Online available at <https://www.dagstuhl.de/dagpub/978-3-95977-370-6>.

*Publication date*

June, 2025

*Bibliographic information published by the Deutsche Nationalbibliothek*

The Deutsche Nationalbibliothek lists this publication in the Deutsche Nationalbibliografie; detailed bibliographic data are available in the Internet at <https://portal.dnb.de>.

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Digital Object Identifier: 10.4230/LIPIcs.SoCG.2025.0



**ISBN 978-3-95977-370-6**

**ISSN 1868-8969**

**<https://www.dagstuhl.de/lipics>**

**PRINT ISBN 979-8-3313-2287-8**

## ■ Contents

Preface	
<i>Oswin Aichholzer and Haitao Wang</i> .....	0:xi–0:xii
Conference Organization	
.....	0:xiii–0:xv
Additional Reviewers	
.....	0:xvii–0:xxii

### Regular Papers

Reconfiguration of Unit Squares and Disks: PSPACE-Hardness in Simple Settings <i>Mikkel Abrahamsen, Kevin Buchin, Maike Buchin, Linda Kleist, Maarten Löffler, Lena Schlipf, André Schulz, and Jack Stade</i> .....	1:1–1:18
The Maximum Number of Digons Formed by Pairwise Intersecting Pseudocircles <i>Eyal Ackerman, Gábor Damásdi, Balázs Keszegh, Rom Pinchasi, and Rebeka Raffay</i>	2:1–2:14
Convexity Helps Iterated Search in 3D <i>Peyman Afshani, Yakov Nekrich, and Frank Staals</i> .....	3:1–3:14
A Subquadratic Algorithm for Computing the $L_1$ -Distance Between Two Terrains <i>Pankaj K. Agarwal, Boris Aronov, Olivier Devillers, Christian Knauer, and Guillaume Moroz</i> .....	4:1–4:17
Optimal Motion Planning for Two Square Robots in a Rectilinear Environment <i>Pankaj K. Agarwal, Mark de Berg, Benjamin Holmgren, Alex Steiger, and Martijn Struijs</i> .....	5:1–5:17
A Sparse Multicover Bifiltration of Linear Size <i>Ángel Javier Alonso</i> .....	6:1–6:18
Single-Source Shortest Path Problem in Weighted Disk Graphs <i>Shinwoo An, Eunjin Oh, and Jie Xue</i> .....	7:1–7:15
Rapid Mixing of the Flip Chain over Non-Crossing Spanning Trees <i>Konrad Anand, Weiming Feng, Graham Freifeld, Heng Guo, Mark Jerrum, and Jiaheng Wang</i> .....	8:1–8:18
Geometric Realizations of Dichotomous Ordinal Graphs <i>Patrizio Angelini, Sabine Cornelsen, Carolina Haase, Michael Hoffmann, Eleni Katsanou, Fabrizio Montecchiani, Raphael Steiner, and Antonios Symvonis</i> .....	9:1–9:16
Steinhaus Filtration and Stable Paths in the Mapper <i>Dustin L. Arendt, Matthew Broussard, Bala Krishnamoorthy, Nathaniel Saul, and Amber Thrall</i> .....	10:1–10:21
When Alpha-Complexes Collapse onto Codimension-1 Submanifolds <i>Dominique Attali, Mattéo Clémot, Bianca B. Dornelas, and André Lieutier</i> .....	11:1–11:19
Higher-Order Color Voronoi Diagrams and the Colorful Clarkson–Shor Framework <i>Sang Won Bae, Nicolau Oliver, and Evanthia Papadopoulou</i> .....	12:1–12:19



The Erdős–Szekeres Conjecture Revisited <i>Jineon Baik and Martin Balko</i> .....	13:1–13:15
Extremal Betti Numbers and Persistence in Flag Complexes <i>Lies Beers and Magnus Bakke Botnan</i> .....	14:1–14:18
When Distances Lie: Euclidean Embeddings in the Presence of Outliers and Distance Violations <i>Matthias Bentert, Fedor V. Fomin, Petr A. Golovach, M. S. Ramanujan, and Saket Saurabh</i> .....	15:1–15:16
Signotopes with Few Plus Signs <i>Helena Bergold, Lukas Egeling, and Hung P. Hoang</i> .....	16:1–16:14
Sparse Bounded Hop-Spanners for Geometric Intersection Graphs <i>Sujoy Bhore, Timothy M. Chan, Zhengcheng Huang, Shakhar Smorodinsky, and Csaba D. Tóth</i> .....	17:1–17:15
Finding a Shortest Curve That Separates Few Objects from Many <i>Therese Biedl, Éric Colin de Verdière, Fabrizio Frati, Anna Lubiw, and Günter Rote</i> .....	18:1–18:16
Polychromatic Coloring of Tuples in Hypergraphs <i>Ahmad Biniaz, Jean-Lou De Carufel, Anil Maheshwari, Michiel Smid, Shakhar Smorodinsky, and Miloš Stojaković</i> .....	19:1–19:17
Polynomial-Time Algorithms for Contiguous Art Gallery and Related Problems <i>Ahmad Biniaz, Anil Maheshwari, Magnus Christian Ring Merrild, Joseph S. B. Mitchell, Saeed Odak, Valentin Polishchuk, Eliot W. Robson, Casper Moldrup Rysgaard, Jens Kristian Refsgaard Schou, Thomas Shermer, Jack Spalding-Jamieson, Rolf Svenning, and Da Wei Zheng</i> .....	20:1–20:21
Structure and Independence in Hyperbolic Uniform Disk Graphs <i>Thomas Bläsius, Jean-Pierre von der Heydt, Sándor Kisfaludi-Bak, Marcus Wilhelm, and Geert van Wordragen</i> .....	21:1–21:16
Transforming Dogs on the Line: On the Fréchet Distance Under Translation or Scaling in 1D <i>Lotte Blank, Jacobus Conradi, Anne Driemel, Benedikt Kolbe, André Nusser, and Marena Richter</i> .....	22:1–22:16
On the Twin-Width of Smooth Manifolds <i>Édouard Bonnet and Kristóf Huszár</i> .....	23:1–23:16
An 11/6-Approximation Algorithm for Vertex Cover on String Graphs <i>Édouard Bonnet and Paweł Rzążewski</i> .....	24:1–24:15
Approximating Klee’s Measure Problem and a Lower Bound for Union Volume Estimation <i>Karl Bringmann, Kasper Green Larsen, André Nusser, Eva Rotenberg, and Yanheng Wang</i> .....	25:1–25:16
Geometric Spanners of Bounded Tree-Width <i>Kevin Buchin, Carolin Rehs, and Torben Scheele</i> .....	26:1–26:15

Computing Oriented Spanners and Their Dilation  
*Kevin Buchin, Antonia Kalb, Anil Maheshwari, Saeed Odak, Carolin Rehs, Michiel Smid, and Sampson Wong* ..... 27:1–27:17

Small Triangulations of 4-Manifolds and the 4-Manifold Census  
*Rhuidi Antonio Burke, Benjamin A. Burton, and Jonathan Spreer* ..... 28:1–28:16

Sparsification of the Generalized Persistence Diagrams for Scalability Through Gradient Descent  
*Mathieu Carrière, Seunghyun Kim, and Woojin Kim* ..... 29:1–29:17

Computation of Toroidal Schnyder Woods Made Simple and Fast: From Theory to Practice  
*Luca Castelli Aleardi, Eric Fusy, Jyh-Chwen Ko, and Razvan-Stefan Puscasu* .... 30:1–30:19

A Linear Time Algorithm for the Maximum Overlap of Two Convex Polygons Under Translation  
*Timothy M. Chan and Isaac M. Hair* ..... 31:1–31:16

Faster Algorithms for Reverse Shortest Path in Unit-Disk Graphs and Related Geometric Optimization Problems: Improving the Shrink-And-Bifurcate Technique  
*Timothy M. Chan and Zhengcheng Huang* ..... 32:1–32:14

On Zarankiewicz’s Problem for Intersection Hypergraphs of Geometric Objects  
*Timothy M. Chan, Chaya Keller, and Shakhar Smorodinsky* ..... 33:1–33:14

Simplification of Trajectory Streams  
*Siu-Wing Cheng, Haoqiang Huang, and Le Jiang* ..... 34:1–34:14

A Theory of Sub-Barcodes  
*Oliver A. Chubet, Kirk P. Gardner, and Donald R. Sheehy* ..... 35:1–35:16

Strongly Sublinear Separators and Bounded Asymptotic Dimension for Sphere Intersection Graphs  
*James Davies, Agelos Georgakopoulos, Meike Hatzel, and Rose McCarty* ..... 36:1–36:16

Nearest Neighbor Searching in a Dynamic Simple Polygon  
*Sarita de Berg and Frank Staals* ..... 37:1–37:15

An Algorithm for Tambara-Yamagami Quantum Invariants of 3-Manifolds, Parameterized by the First Betti Number  
*Colleen Delaney, Clément Maria, and Eric Samperton* ..... 38:1–38:15

Tiling with Three Polygons Is Undecidable  
*Erik D. Demaine and Stefan Langerman* ..... 39:1–39:16

Apex Representatives  
*Tamal K. Dey, Tao Hou, and Dmitriy Morozov* ..... 40:1–40:16

Decomposing Multiparameter Persistence Modules  
*Tamal K. Dey, Jan Jendrysiak, and Michael Kerber* ..... 41:1–41:19

Range Counting Oracles for Geometric Problems  
*Anne Driemel, Morteza Monemizadeh, Eunjin Oh, Frank Staals, and David P. Woodruff* ..... 42:1–42:16

On Spheres with $k$ Points Inside <i>Herbert Edelsbrunner, Alexey Garber, and Morteza Saghafian</i> .....	43:1–43:12
A Minor-Testing Approach for Coordinated Motion Planning with Sliding Robots <i>Eduard Eiben, Robert Ganian, Iyad Kanj, and M. S. Ramanujan</i> .....	44:1–44:15
Higher Order Bipartiteness vs Bi-Partitioning in Simplicial Complexes <i>Marzieh Eidi and Sayan Mukherjee</i> .....	45:1–45:12
Non-Euclidean Erdős–Anning Theorems <i>David Eppstein</i> .....	46:1–46:15
Shelling and Sinking Graphs on the Sphere <i>Jeff Erickson and Christian Howard</i> .....	47:1–47:18
Exact Algorithms for Minimum Dilation Triangulation <i>Sándor P. Fekete, Phillip Keldenich, and Michael Perk</i> .....	48:1–48:18
On Sparse Covers of Minor Free Graphs, Low Dimensional Metric Embeddings, and Other Applications <i>Arnold Filtser</i> .....	49:1–49:16
Immersions and Albertson’s Conjecture <i>Jacob Fox, János Pach, and Andrew Suk</i> .....	50:1–50:10
Quantum Combine and Conquer and Its Applications to Sublinear Quantum Convex Hull and Maxima Set Construction <i>Shion Fukuzawa, Michael T. Goodrich, and Sandy Irani</i> .....	51:1–51:15
Uniform Bounds on Product Sylvester-Gallai Configurations <i>Abhibhav Garg, Rafael Oliveira, and Akash Kumar Sengupta</i> .....	52:1–52:15
A PTAS for TSP with Neighbourhoods over Parallel Line Segments <i>Benjamin Ghasemini and Mohammad R. Salavatipour</i> .....	53:1–53:15
The Fréchet Distance Unleashed: Approximating a Dog with a Frog <i>Sariel Har-Peled, Benjamin Raichel, and Eliot W. Robson</i> .....	54:1–54:13
A Practical Algorithm for Knot Factorisation <i>Alexander He, Eric Sedgwick, and Jonathan Spreer</i> .....	55:1–55:15
Sublinear Data Structures for Nearest Neighbor in Ultra High Dimensions <i>Martin G. Herold, Danupon Nanongkai, Joachim Spoerhase, Nithin Varma, and Zihang Wu</i> .....	56:1–56:15
Snap Rounding: A Cautionary Tale <i>John Hershberger</i> .....	57:1–57:14
Tracking the Persistence of Harmonic Chains: Barcode and Stability <i>Tao Hou, Salman Parsa, and Bei Wang</i> .....	58:1–58:16
Incremental Planar Nearest Neighbor Queries with Optimal Query Time <i>John Iacono and Yakov Nekrich</i> .....	59:1–59:15
Improved Approximation Algorithms for Three-Dimensional Knapsack <i>Klaus Jansen, Debajyoti Kar, Arindam Khan, K. V. N. Sreenivas, and Malte Tutas</i>	60:1–60:18

<i>k</i> -Dimensional Transversals for Fat Convex Sets <i>Attila Jung and Dömötör Pálvölgyi</i> .....	61:1–61:12
On Approximability of $\ell_2^2$ Min-Sum Clustering <i>Karthik C. S., Euiwoong Lee, Yuval Rabani, Chris Schwiegelshohn, and Samson Zhou</i> .....	62:1–62:18
The Maximum Clique Problem in a Disk Graph Made Easy <i>J. Mark Keil and Debajyoti Mondal</i> .....	63:1–63:16
Super-Polynomial Growth of the Generalized Persistence Diagram <i>Donghan Kim, Woojin Kim, and Wonjun Lee</i> .....	64:1–64:20
Recognizing 2-Layer and Outer <i>k</i> -Planar Graphs <i>Yasuaki Kobayashi, Yuto Okada, and Alexander Wolff</i> .....	65:1–65:16
Lipschitz Decompositions of Finite $\ell_p$ Metrics <i>Robert Krauthgamer and Nir Petruschka</i> .....	66:1–66:14
Hard Diagrams of Split Links <i>Corentin Lunel, Arnaud de Mesmay, and Jonathan Spreer</i> .....	67:1–67:17
Persistent (Co)Homology in Matrix Multiplication Time <i>Dmitriy Morozov and Primož Skraba</i> .....	68:1–68:16
Computing Betti Tables and Minimal Presentations of Zero-Dimensional Persistent Homology <i>Dmitriy Morozov and Luis Scoccola</i> .....	69:1–69:15
Computing Geomorphologically Salient Networks via Discrete Morse Theory <i>Tim Ophelders, Anna Schenfisch, Willem Sonke, and Bettina Speckmann</i> .....	70:1–70:17
Banana Trees for the Persistence in Time Series Experimentally <i>Lara Ost, Sebastiano Cultrera di Montesano, and Herbert Edelsbrunner</i> .....	71:1–71:13
Geometric Bipartite Matching Based Exact Algorithms for Server Problems <i>Sharath Raghvendra, Pouyan Shirzadian, and Rachita Sowle</i> .....	72:1–72:15
Embedding Graphs as Euclidean <i>k</i> NN-Graphs <i>Thomas Schibler, Subhash Suri, and Jie Xue</i> .....	73:1–73:14
The Point-Boundary Art Gallery Problem Is $\exists\mathbb{R}$ -Hard <i>Jack Stade</i> .....	74:1–74:23
Levels in Arrangements: Linear Relations, the <i>g</i> -Matrix, and Applications to Crossing Numbers <i>Elizaveta Streltsova and Uli Wagner</i> .....	75:1–75:18
A Note on the No- $(d + 2)$ -On-a-Sphere Problem <i>Andrew Suk and Ethan Patrick White</i> .....	76:1–76:8
Dynamic Maximum Depth of Geometric Objects <i>Subhash Suri, Jie Xue, Xiongxin Yang, and Jiumu Zhu</i> .....	77:1–77:13
Efficient Greedy Discrete Subtrajectory Clustering <i>Ivor van der Hoog, Lara Ost, Eva Rotenberg, and Daniel Rutschmann</i> .....	78:1–78:20

## CG Challenges

Computing Non-Obtuse Triangulations with Few Steiner Points <i>Mikkel Abrahamsen, Florestan Brunck, Jacobus Conradi, Benedikt Kolbe, and André Nusser</i> .....	79:1–79:13
Incremental Algorithm and Local Search for Minimum Non-Obtuse Triangulations <i>Tae-hoon Ahn, Jaegun Lee, Byeonguk Kang, and Hwi Kim</i> .....	80:1–80:8

## Media Expositions

AmoebotSim 2.0: A Visual Simulation Environment for the Amoebot Model with Reconfigurable Circuits and Joint Movements <i>Matthias Artmann, Tobias Maurer, Andreas Padalkin, Daniel Warner, and Christian Scheideler</i> .....	81:1–81:5
Software for the Thompson and Funk Polygonal Geometry <i>Hridhaan Banerjee, Carmen Isabel Day, Auguste H. Gezalayan, Olga Golovatskaia, Megan Hunleth, Sarah Hwang, Nithin Parepally, Lucy Wang, and David M. Mount</i>	82:1–82:6
French Onion Soup, Ipelets for Points and Polygons <i>Klint Faber, Auguste H. Gezalayan, Adam Martinson, Aniruddh Mutnuru, Nithin Parepally, Ryan Parker, Mihil Sreenilayam, Aram Zaproshyan, and David M. Mount</i> .....	83:1–83:6
Incremental and Interactive PQ- and PC-Trees <i>Simon D. Fink and Dominik Peters</i> .....	84:1–84:4
Finding Shortest Reconfiguration Sequences for Modular Robots <i>UML Modular Robotics Group, Hugo A. Akitaya, Andrew Clements, Sam Downey, Jonathan Eisenbies, Soham Samanta, Gabriel Shahrouzi, and Frederick Stock</i> ....	85:1–85:5