
LLM at Network Edge: A Layer-wise Efficient Federated Fine-tuning Approach

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Abstract

Fine-tuning large language models (LLMs) poses significant computational burdens, especially in federated learning (FL) settings. We introduce Layer-wise Efficient Federated Fine-tuning (LEFF), a novel method designed to enhance the efficiency of FL fine-tuning while preserving model performance and minimizing client-side computational overhead. LEFF strategically selects layers for fine-tuning based on client computational capacity, thereby mitigating the straggler effect prevalent in heterogeneous environments. Furthermore, LEFF incorporates an importance-driven layer sampling mechanism, prioritizing layers with greater influence on model performance. Theoretical analysis demonstrates that LEFF achieves a convergence rate of $\mathcal{O}(1/\sqrt{T})$. Extensive experiments on diverse datasets demonstrate that LEFF attains superior computational efficiency and model performance compared to existing federated fine-tuning methods, particularly under heterogeneous conditions.

1 Introduction

Large Language Models (LLMs)² have exhibited remarkable capabilities in various downstream tasks, including text generation Li et al. (2024), language translation Ranathunga et al. (2023), and question answering Yu et al. (2024). Their success is primarily attributed to their increasing model scale Bahri et al. (2024), with contemporary models scaling from billions of parameters (e.g., GPT-2) to hundreds of billions (e.g., GPT-4). While fine-tuning pre-trained LLMs on task-specific data is the de facto approach for adaptation, the privacy-sensitive nature of user-generated data poses challenges to centralized collection. Federated learning (FL) offers a solution by enabling distributed model training without requiring data centralization McMahan et al. (2017); Huang et al. (2024). In FL, models are fine-tuned directly on user devices, thereby preserving data privacy. However, the computational demands of fine-tuning such large models often surpass the capabilities of typical consumer devices. For instance, while typical consumer GPUs are often limited to 24GB of graphics memory, fine-tuning a GPT-3 model even with 16-bit precision requires approximately 326GB of memory.

Addressing the significant computational demands of LLMs, researchers have explored various mitigation strategies Han et al. (2024). parameter-efficient fine-tuning (PEFT) methods, including Adapter Housby et al. (2019), LoRA Hu et al. (2022), and prompt tuning Lester et al. (2021), have

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²In this paper, we focus on transformer-based language models. For simplicity, we refer to transformer blocks as layers.

emerged as promising approaches. These methods fine-tune a small number of additional or selected parameters while keeping the bulk of the pre-trained model frozen, thereby substantially reducing computational overhead. However, applying PEFT methods within FL settings encounters several critical challenges. First, the non-independent and identically distributed (non-IID) nature of client data is a primary concern Qi et al. (2023), often leading to substantial performance degradation Huang et al. (2023, 2022). This degradation can be particularly pronounced in federated PEFT compared to full fine-tuning paradigms Babakniya et al. (2023). Additionally, computational heterogeneity across participating devices impairs resource utilization efficiency due to the *straggler effect*, where overall training progress is constrained by the slowest clients Shen et al. (2024). While recent approaches, such as FedDSE, explore sub-model extraction based on neuron activation patterns for resource-constrained FL Wang et al. (2024a), maintaining model performance under non-IID data distributions remains a significant hurdle.

To address these challenges, we propose **Layer-wise Efficient Federated Fine-tuning (LEFF)**, a method that aims to preserve the efficacy of full-parameter fine-tuning while significantly reducing computational overhead. LEFF enables clients to selectively fine-tune specific layers according to their computational capacity, while other layers remain frozen during local training. This flexibility allows resource-constrained clients to fine-tune a reduced set of layers, thereby mitigating the straggler effect. Following local training, clients transmit only the updated parameters of their selected layers to the server. The server then performs layer-wise aggregation to reconstruct the global model for the subsequent round. To further optimize the fine-tuning process, we introduce an importance-based layer sampling strategy. This strategy dynamically adjusts the selection probability of each layer based on its contribution to overall fine-tuning performance. This approach ensures that more impactful layers are prioritized for updates. Our key contributions are:

- **Novel Architecture:** We introduce LEFF, a federated fine-tuning framework designed to preserve full-parameter fine-tuning efficacy while substantially mitigating client-side computational overhead.
- **Robustness to Data Heterogeneity:** LEFF leverages full-parameter fine-tuning, enabling superior adaptation to non-IID data distributions across clients, outperforming conventional PEFT methods like LoRA.
- **Computational Heterogeneity Mitigation:** Our framework accommodates computational heterogeneity by allowing clients to dynamically adjust their local training workload according to their available resources, thereby mitigating the straggler problem.
- **Adaptive Layer Prioritization:** We develop an adaptive layer selection mechanism employing an importance-based sampling algorithm. This prioritizes updates for performance-critical layers, enhancing both training efficiency and model effectiveness.
- **Theoretical Guarantees:** We provide a rigorous convergence analysis, demonstrating that LEFF achieves a convergence rate of $\mathcal{O}(1/\sqrt{T})$.
- **Empirical Validation:** Extensive experiments demonstrate LEFF's capability to significantly reduce client-side computational burden while achieving superior fine-tuning performance under heterogeneous data and system conditions, outperforming existing state-of-the-art methods.

The remainder of this paper is organized as follows. Section 2 reviews the relevant literature on FL and PEFT. Section 3 details our proposed LEFF framework and its key components. Section 4 provides a convergence analysis. Section 5 presents comprehensive experimental results and analyses. Finally, Section 6 summarizes our findings and discusses future work.

2 Related Work

PEFT methods are essential for adapting LLMs by alleviating the prohibitive computational costs of full fine-tuning. Techniques have evolved from updating parameter subsets Zaken et al. (2021) and injecting trainable modules Houlsby et al. (2019) to latency-free approaches like LoRA Hu et al. (2022); Fu et al. (2022), which merges learned low-rank matrices into the original model. Further refinements, such as dynamically updating important layers as demonstrated by LISA Pan et al. (2024), optimize efficiency by targeting model capacity more effectively. While established in centralized

settings, PEFT's application to FL is an emerging research area Zhuang et al. (2023); Yu et al. (2023); Woisetschlager et al. (2024). Various PEFT strategies, including LoRA-based instruction tuning Zhang et al. (2024), federated prompt optimization Guo et al. (2023, 2024), and backpropagation-free client fine-tuning Xu et al. (2023), have shown viability in FL Chen et al. (2022, 2023); Sun et al. (2022); Zhang et al. (2023); Fang et al. (2024); Legate et al. (2023); Wang et al. (2024b). However, a critical challenge is data heterogeneity across clients, which analyses confirm significantly degrades PEFT performance compared to full fine-tuning Babakniya et al. (2023); Bai et al. (2024); Cho et al. (2023), a limitation even for specialized approaches like FedDAT in multimodal tasks Chen et al. (2024). Concurrently, federated full-parameter tuning methods present their own trade-offs, including high client computation in gradient approximation Qin et al. (2024), unreduced peak memory load in update-compression schemes Shu et al. (2025), and a lack of adaptability in static cyclical updates Wang et al. (2024c). To address this performance degradation, we propose LEFF. Unlike prior work, LEFF facilitates decentralized, layer-wise adaptation of backbone models by enabling client-specific full-parameter updates to a selected subset of layers, aiming to effectively mitigate the adverse impacts of data heterogeneity while preserving computational efficiency.

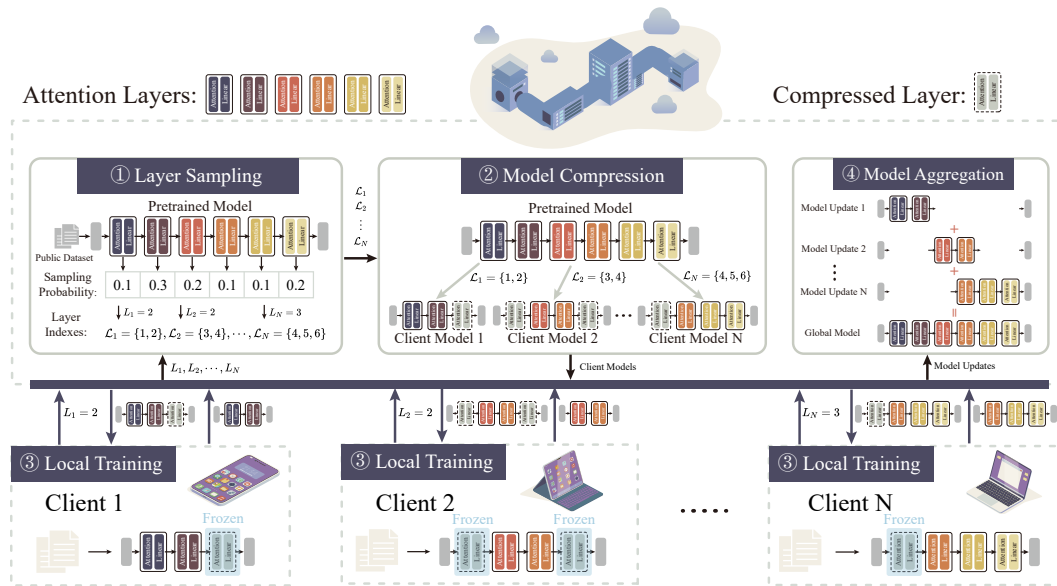


Figure 1: Overview of the LEFF framework. Each communication round comprises four key stages.

3 Methodology

3.1 System Architecture

FL clients in edge computing (e.g., mobile phones, personal computers) often possess limited computational resources. The increasing scale of LLMs intensifies this constraint, making their fine-tuning computationally burdensome. To mitigate this, we introduce LEFF, a framework to reduce client-side training overhead while striving to maintain the benefits of full-parameter fine-tuning.

The LEFF framework (Figure 1) involves four steps per communication round. First, clients report their local fine-tuning capacity (number of layers L_i). Based on these reports, the server calculates sampling probabilities and selects a layer subset $\mathcal{L}_i$ (of size L_i) for each client $\mathcal{C}_i$ to fine-tune. Second, to reduce client burden, the server compresses unselected layers $\mathcal{L}_i^-$ via knowledge distillation, creating a customized local model. This model comprises client-specific fine-tunable layers (from $\mathcal{L}_i$) and frozen compressed layers (derived from $\mathcal{L}_i^-$). Third, clients fine-tune only their assigned layers; other compressed layers remain frozen. Finally, clients upload their fine-tuned layer parameters, and the server performs layer-wise aggregation to update the global model.

We consider a standard FL setup: a central server aggregates parameters from N clients ($\mathcal{C}_i, i = 1, \dots, N$) performing local training on their datasets $\mathcal{D}_i$ (size $D_i = |\mathcal{D}_i|$). The global model Θ_g has L layers. For each client $\mathcal{C}_i$, the server samples a block of L_i consecutive layers for fine-tuning,

denoted $\mathcal{L}_i$:

$$\mathcal{L}_i = \{l_{\text{start}}, \dots, l_{\text{end}}\}, \quad \text{s.t.} \quad l_{\text{end}} - l_{\text{start}} + 1 = L_i. \quad (1)$$

The unselected layers $\mathcal{L}_i^- = \{l_k \mid 1 \leq l_k \leq L, l_k \notin \mathcal{L}_i\}$ are compressed by the server into $\check{\Theta}_g^{\mathcal{L}_i^-}$. The resulting client-specific model $\Theta_i = \{\Theta_g^{\mathcal{L}_i}, \check{\Theta}_g^{\mathcal{L}_i^-}\}$ supports forward propagation. Client $\mathcal{C}_i$ receives Θ_i , fine-tunes only $\Theta_g^{\mathcal{L}_i}$ on $\mathcal{D}_i$ to obtain updated parameters $\Theta_i^{\mathcal{L}_i}$ (while $\check{\Theta}_g^{\mathcal{L}_i^-}$ remain frozen), and uploads $\Theta_i^{\mathcal{L}_i}$. The server aggregates these layer-specific parameters from all clients to update Θ_g .

3.2 Layer Sampling

At the start of each communication round, the server selects the layers for each client to fine-tune based on L_i . Considering that layers contribute differently to fine-tuning performance, we propose an importance-based layer sampling method. This approach prioritizes layers considered more crucial for model fine-tuning, thereby optimizing the fine-tuning process by concentrating computational resources on the most impactful model parts.

As discussed in Molchanov et al. (2019), the importance of a neural parameter can be quantified by the change in the loss value when the parameter is introduced or removed:

$$\mathcal{I}_m = (\mathcal{F}(\mathcal{D}, \Theta) - \mathcal{F}(\mathcal{D}, \Theta|_{\theta_m=0}))^2, \quad (2)$$

where $\mathcal{F}$ denotes the loss function, $\mathcal{D}$ represents the dataset, and θ_m is the m -th parameter of the model Θ . We further adopt its first-order Taylor expansion form:

$$\mathcal{I}_m^{(1)}(\Theta) = (g_m \theta_m)^2, \quad (3)$$

where g_m is the gradient of the m -th parameter. This approximation allows for estimating each parameter's importance with only a single forward and backward pass, significantly reducing computational complexity.

As illustrated in Figure 2. Based on the importance scores of individual parameters, the importance score for each layer can be derived by summing the importance scores of all parameters within that layer:

$$\mathcal{I}_{\Theta^l} \approx \mathcal{I}_{\Theta^l}^{(1)}(\Theta) = \sum_{m \in \Theta^l} \mathcal{I}_m^{(1)}(\Theta) = \sum_{m \in \Theta^l} (g_m \theta_m)^2 \quad (4)$$

We define consecutive L_i layers as a *block*, denoted as $\bar{\Theta}^k = \{\Theta^k, \dots, \Theta^{k+L_i-1}\}$, with its importance given by:

$$\mathcal{I}_{\bar{\Theta}^k} = \sum_{l=k}^{k+L_i-1} \mathcal{I}_{\Theta^l} \quad (5)$$

To determine the sampling probability, these importance scores are normalized using the Softmax function. Thus, the sampling probability for each block during layer sampling for client $\mathcal{C}_i$ is expressed as:

$$\mathbf{p}_i = \text{Softmax}(\{\mathcal{I}_{\bar{\Theta}^k} \mid k = 1, \dots, L - L_i + 1\}) \quad (6)$$

The server utilizes $\mathbf{p}_i$ to sample a block for client $\mathcal{C}_i$, determining the set of layers $\mathcal{L}_i$ that the client will fine-tune in the current communication round.

3.3 Model Compression

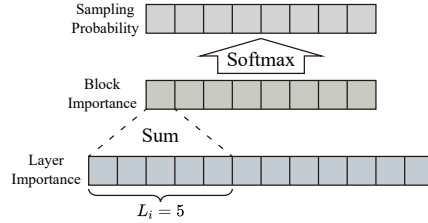


Figure 2: Sampling probability for each block. Model layers are organized into blocks, and clients sample only one block per communication round for fine-tuning.

As illustrated in Figure 3, in each communication round, prior to client-side fine-tuning, the server compresses the layers not selected for client fine-tuning, denoted by $\mathcal{L}_i^-$, to reduce computational overhead. Specifically, the server employs a proxy dataset $\mathcal{D}_{\text{proxy}}$, sourced from publicly available data, for this knowledge distillation process. The student model $\check{\Theta}_g^{\mathcal{L}_i^-}$ maintains a multi-layer attention architecture identical to that of the corresponding layers in the pre-trained global model. The number of layers in the student model is determined by a compression rate r . If the teacher model segment $\Theta_g^{\mathcal{L}_i^-}$ comprises $|\Theta_g^{\mathcal{L}_i^-}|$ layers, the student model's layer count is $|\check{\Theta}_g^{\mathcal{L}_i^-}| = \lceil |\Theta_g^{\mathcal{L}_i^-}| \cdot r \rceil$.

Once the student model's architecture is defined, the server initiates compression via knowledge distillation. This distillation leverages two objectives: a Mean Squared Error (MSE) loss between the hidden states of the teacher and student models, and a Kullback-Leibler (KL) divergence between their attention matrices. Crucially, to prevent the student model from learning task-irrelevant information from $\mathcal{D}_{\text{proxy}}$, only the intermediate representations (hidden states and attention matrices) are used for distillation, not the task-specific output labels from $\mathcal{D}_{\text{proxy}}$. Specifically, for an input hidden state sequence H_i , the teacher model segment $\Theta_g^{\mathcal{L}_i^-}$ produces outputs $(H_t, A_t) = \Theta_g^{\mathcal{L}_i^-}(H_i)$, while the student model $\check{\Theta}_g^{\mathcal{L}_i^-}$ produces $(H_s, A_s) = \check{\Theta}_g^{\mathcal{L}_i^-}(H_i)$. The distillation loss E_{distill} is then formulated as:

$$E_{\text{distill}} = (1 - \alpha)E_{\text{hidden_state}} + \alpha E_{\text{attention_matrix}} = (1 - \alpha)\text{MSE}(H_t, H_s) + \alpha \text{KL}(A_t, A_s), \quad (7)$$

where α is a hyperparameter balancing the two loss components. Following compression, the server integrates the student model $\check{\Theta}_g^{\mathcal{L}_i^-}$ with the layers selected for fine-tuning, $\Theta_g^{\mathcal{L}_i}$, to form the client-specific model $\Theta_i = \{\Theta_g^{\mathcal{L}_i}, \check{\Theta}_g^{\mathcal{L}_i^-}\}$. This model Θ_i is then dispatched to the i -th client.

3.4 Local Training

Upon receiving the model Θ_i from the server, client $\mathcal{C}_i$ fine-tunes the selected layers $\Theta_g^{\mathcal{L}_i}$, while the unselected layers $\check{\Theta}_g^{\mathcal{L}_i^-}$ remain frozen to maintain the correct training context. This strategy enables clients to update only a subset of parameters, with the compressed unselected parameters requiring minimal resources. As a result, LEFF significantly reduces computational overhead on the client side, and adapts to the client's computational capabilities, thereby enhancing efficiency. After completing local training, client $\mathcal{C}_i$ sends the updated model parameters $\Theta_i^{\mathcal{L}_i}$ back to the server for aggregation.

3.5 Model Aggregation

After receiving model parameters from all clients, the server aggregates them to construct a comprehensive global model. Since each client fine-tunes different components of the model, we utilize a layer-wise aggregation approach, performing weighted averaging for each layer individually. Specifically, for a global model $\Theta_g = \{\Theta_g^1, \dots, \Theta_g^L\}$ with L layers, let $\mathcal{S}_l$ represent the set of clients that fine-tuned the l -th layer. The aggregated global model is expressed as follows:

$$\Theta_g = \{\Theta_g^l \mid l = 1, \dots, L\} = \left\{ \sum_{i \in \mathcal{S}_l} \frac{D_i}{\sum_{j \in \mathcal{S}_l} D_j} \Theta_i^l \mid l = 1, \dots, L \right\}. \quad (8)$$

Once the server completes the aggregation and acquires the updated global model, the subsequent communication round commences. This process continues until the model converges or reaches a predetermined number of iterations.

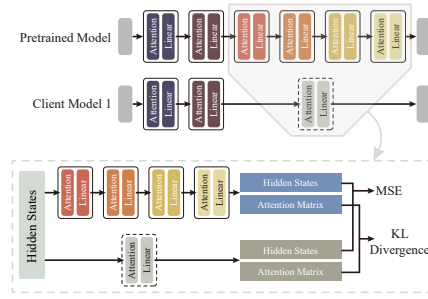


Figure 3: Distillation process in LEFF. The distillation loss comprises two components: the mean square loss of the hidden state and the KL divergence of the attention matrix.

4 Convergence Analysis

4.1 Assumptions

Our convergence analysis of LEFF relies on the following assumptions. Assumptions 1,2,3 are standard in FL (Li et al., 2020); Assumption 4 addresses complexities from LEFF's layer selection and model compression.

Assumption 1 (L-Smoothness). *Each client's local loss function $\mathcal{F}_i : \mathbb{R}^d \rightarrow \mathbb{R}$ is L -smooth with respect to the full model parameters Θ . Thus, for a constant $L > 0$, all $\Theta_1, \Theta_2 \in \mathbb{R}^d$, and all clients $i \in [N]$:*

$$\|\nabla \mathcal{F}_i(\Theta_1) - \nabla \mathcal{F}_i(\Theta_2)\| \leq L\|\Theta_1 - \Theta_2\|. \quad (9)$$

The global loss function $\mathcal{F}(\Theta) = \frac{1}{N} \sum_{i=1}^N \mathcal{F}_i(\Theta)$ is thus also L -smooth.

Assumption 2 (Bounded Variance). *The variance of stochastic gradients computed by each client is bounded. Let $\nabla \mathcal{F}_i(\Theta; \xi)$ be client i 's stochastic gradient for sample $\xi \sim \mathcal{D}_i$ at parameters Θ , and $\nabla \mathcal{F}_i(\Theta) = \mathbb{E}_{\xi \sim \mathcal{D}_i}[\nabla \mathcal{F}_i(\Theta; \xi)]$ be the true local gradient. We assume constants $\sigma_i^2 \geq 0$ such that for all $\Theta \in \mathbb{R}^d$ and $i \in [N]$:*

$$\mathbb{E}_{\xi \sim \mathcal{D}_i} \|\nabla \mathcal{F}_i(\Theta; \xi) - \nabla \mathcal{F}_i(\Theta)\|^2 \leq \sigma_i^2. \quad (10)$$

We define $\sigma^2 = \max_{i \in [N]} \sigma_i^2$. This is standard in analyzing stochastic optimization, including FL.

Assumption 3 (Bounded Heterogeneity). *To account for data heterogeneity (non-IID data), we assume the dissimilarity between true local and global gradients is bounded. For a constant $\zeta^2 \geq 0$ and all $\Theta \in \mathbb{R}^d$:*

$$\frac{1}{N} \sum_{i=1}^N \|\nabla \mathcal{F}_i(\Theta) - \nabla \mathcal{F}(\Theta)\|^2 \leq \zeta^2. \quad (11)$$

This is standard in FL analysis, especially for non-IID settings.

During local training in round t , client i performs K steps of stochastic gradient descent, starting from $\Theta_{i,t,0}^{\mathcal{L}_i} = \Theta_{g,t}^{\mathcal{L}_i}$. At local step $k \in \{0, \dots, K-1\}$, the client updates $\Theta_{i,t,k}^{\mathcal{L}_i}$ using a stochastic gradient $G_{i,t,k}$ computed with respect to these active parameters:

$$G_{i,t,k} = \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{i,t,k}^{\mathcal{L}_i} | \check{\Theta}_{g,t}^{\mathcal{L}_i^-}; \xi_{i,t,k}). \quad (12)$$

Here, $\mathcal{F}_i(\cdot; \xi)$ indicates the loss evaluated with active parameters $\Theta_{i,t,k}^{\mathcal{L}_i}$ conditioned on the fixed context $\check{\Theta}_{g,t}^{\mathcal{L}_i^-}$, using data sample $\xi_{i,t,k} \sim \mathcal{D}_i$.

Let $\bar{G}_{i,t}$ be the average expected effective gradient computed by client i over its K local steps in round t :

$$\bar{G}_{i,t} = \frac{1}{K} \sum_{k=0}^{K-1} \mathbb{E}_{\xi_{i,t,k} \sim \mathcal{D}_i} [G_{i,t,k}]. \quad (13)$$

Let $\nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t})$ denote the restriction of the full local gradient $\nabla \mathcal{F}_i(\Theta_{g,t})$ to the subspace corresponding to the selected layers $\mathcal{L}_i$.

Assumption 4 (Bounded Model Approximation Error). *The expected squared norm difference between the average effective gradient $\bar{G}_{i,t}$ and the corresponding part of the true local gradient $\nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t})$ (evaluated at the start-of-round global model Θ_t^g) is bounded. The expectation $\mathbb{E}_{\mathcal{L}_i \sim \mathbf{p}_i}$ is taken over the randomness of layer selection for client i (with selection distribution $\mathbf{p}_i$):*

$$\mathbb{E}_{\mathcal{L}_i \sim \mathbf{p}_i} [\|\bar{G}_{i,t} - \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t})\|^2] \leq \Delta_{i,t}^2. \quad (14)$$

Furthermore, we assume the average of these client-specific error bounds across all clients is bounded, potentially depending on the round t :

$$\frac{1}{N} \sum_{i=1}^N \Delta_{i,t}^2 \leq \Delta_t^2. \quad (15)$$

For simplicity in certain analyses, one might further assume a uniform bound Δ^2 such that $\Delta_t^2 \leq \Delta^2$ for all t .

4.2 Main Theorem

We present the key lemma leading to our main convergence theorem.

Lemma 1 (Bound on Expected Squared Norm of Global Update). *Let Assumptions 1, 2, 3, and 4 hold. Let $\mathcal{A}_t$ be the set of clients selected in round t . The expected squared norm of the global model change in one communication round t is bounded by:*

$$\mathbb{E} \left[\|\Theta_{t+1}^g - \Theta_t^g\|^2 \right] \leq C_3 \eta^2 K^2 \left(\sigma^2 + \Delta_t^2 + \zeta^2 + \|\nabla \mathcal{F}(\Theta_t^g)\|^2 \right), \quad (16)$$

where the expectation $\mathbb{E}[\cdot]$ is taken over the randomness of client selection $\mathcal{A}_t$, layer selections $\{\mathcal{L}_i\}_{i \in \mathcal{A}_t}$, and local stochastic gradients $\{\xi_{i,t,k}\}_{i \in \mathcal{A}_t, 0 \leq k < K}$. Here, C_3 is a constant that may depend on the total number of layers L , client sampling strategy, layer sampling probabilities $\mathbf{p}_i$, and aggregation weights.

Theorem 1 (Convergence of LEFF). *Let Assumptions 1, 2, 3, and 4 hold. If η is chosen such that $\eta \leq C_4/(LC_3K)$ for sufficiently small C_4 (where C_3 is from Lemma 1, L is the smoothness constant from Assumption 1, and K is the number of local steps), then the LEFF algorithm satisfies:*

$$\frac{1}{T} \sum_{t=0}^{T-1} \mathbb{E}[\|\nabla \mathcal{F}(\Theta_{g,t})\|^2] \leq \underbrace{\frac{C_8(\mathcal{F}(\Theta_{g,0}) - F^*)}{\eta KT}}_{\text{Vanishing term}} + \underbrace{C_9 \left(\bar{\Delta}^2 + \zeta^2 + \frac{\sigma^2}{K} \right) + C_{10}\eta K(\sigma^2 + \bar{\Delta}^2 + \zeta^2)}_{\text{Error floor}}, \quad (17)$$

where $\mathbb{E}[\cdot]$ takes expectation over all randomness up to round t , T is the total number of communication rounds, $\bar{\Delta}^2 = \frac{1}{T} \sum_{t=0}^{T-1} \Delta_t^2$ is the average model approximation error over T rounds, F^* is a lower bound for the global loss function $\mathcal{F}(\Theta)$, and C_8, C_9, C_{10} are positive constants depending on problem parameters (L, σ^2, ζ^2), algorithm parameters (K), and constants from the assumptions and lemmas.

With an appropriately chosen decaying learning rate $\eta = \mathcal{O}(1/\sqrt{T})$ (satisfying the condition in Theorem 1 for sufficiently large T), the bound in Eq. (17) implies a convergence rate where the average squared gradient norm diminishes towards an error floor. This leads to the following corollary regarding the minimum expected gradient norm:

Corollary 1 (Convergence Rate). *Under the conditions of Theorem 1, if a decaying learning rate $\eta = \mathcal{O}(1/\sqrt{T})$ is used, then LEFF achieves:*

$$\min_{0 \leq t \leq T-1} \mathbb{E}[\|\nabla \mathcal{F}(\Theta_{g,t})\|^2] \leq \mathcal{O} \left(\frac{1}{\sqrt{T}} \right) + C_9 \left(\bar{\Delta}^2 + \zeta^2 + \frac{\sigma^2}{K} \right). \quad (18)$$

The convergence is guaranteed only up to an error floor, primarily determined by the non-vanishing term $C_9(\bar{\Delta}^2 + \zeta^2 + \sigma^2/K)$ in Eq. (18). This term quantifies the sources of residual error inherent in the federated optimization process with LEFF.

Trade-offs: The analysis reveals a fundamental trade-off inherent in LEFF. The framework enhances client-side efficiency (computation, memory, potentially communication) through layer selection and context compression. However, this introduces the model approximation error $\bar{\Delta}^2$, which contributes directly to the convergence error floor and may limit the achievable model accuracy. Consequently, the practical success of LEFF hinges on implementing layer selection and compression techniques that effectively minimize $\bar{\Delta}^2$ while preserving the desired efficiency gains.

5 Evaluations

5.1 Experimental Setup

We conduct extensive experiments to evaluate our proposed method against established FL approaches. The evaluation framework incorporates baseline algorithms, pre-trained models, benchmark datasets, and detailed experimental configurations.

We benchmark our approach against FedAvg McMahan et al. (2017), which averages full model parameters, and three parameter-efficient FL methods: FedBitFit Zaken et al. (2021), updating only

bias terms; FedLoRA Hu et al. (2022), employing low-rank updates; and SLoRA Babakniya et al. (2023), utilizing server-side singular value decomposition (SVD) for enhanced stability and efficiency. Experiments are conducted using GPT-2 Medium Radford et al. (2019) for natural language generation (NLG) and DeBERTaV3 Base He et al. (2021) for natural language understanding (NLU). We evaluate on the GLUE benchmark Wang et al. (2019) (e.g., CoLA, MRPC, MNLI) for NLU tasks and the E2E NLG Challenge Novikova et al. (2017) for NLG from structured meaning representations.

Experiments were conducted for 20 communication rounds on the public datasets WebNLG Gardent et al. (2017) and WNLI Wang et al. (2019). To simulate heterogeneous (non-IID) data distributions, client data was partitioned using a Dirichlet distribution with a concentration parameter (α) ranging from 0.05 to 50.0. Our FL simulations involved a varying number of clients, each performing one local training epoch per communication round. During local training, clients fine-tuned their local models using the AdamW optimizer Loshchilov, Hutter (2019) with a learning rate of 1×10^{-5} . All experiments were performed on a system with eight NVIDIA H100 GPUs. This experimental setup enables a systematic evaluation of the proposed method’s robustness against diverse data distributions and varying client participation levels.

5.2 Results

5.2.1 Comparison with Baselines

We evaluate LEFF on the GLUE benchmark across varying data heterogeneity, controlled by the Dirichlet parameter $\alpha \in \{0.05, 0.1, 0.5, 1.0, 5.0, 10.0, 50.0\}$ (Figure 4). While FedAvg’s full-parameter fine-tuning ensures robust performance across all α values, methods relying on partial parameter updates (e.g., FedBitFit, FedLoRA, and SLoRA) exhibit limitations, particularly in highly heterogeneous settings (low α). In contrast, LEFF employs a layer-wise federated fine-tuning strategy, dynamically selecting layers based on client computational capabilities and importance sampling. This approach enables LEFF to achieve consistently strong performance, effectively addressing both data and system heterogeneity and outperforming baselines in critical heterogeneity ranges. Notably, at high data heterogeneity ($\alpha = 0.05$, Table 1), FedAvg attains the highest GLUE scores, with LEFF delivering closely comparable results and also demonstrating competitive performance on NLG tasks.

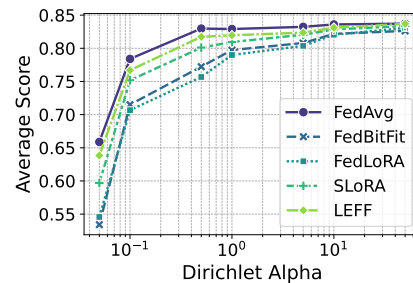


Figure 4: Average score of DeBERTaV3 on GLUE benchmark.

Table 1: Test results of DeBERTaV3 (trained on GLUE tasks) and GPT2 (trained on E2E NLG task). The best result per task group is marked in underline, and the secondary is marked in **bold**.

Model	DeBERTaV3 (GLUE Tasks)									GPT2 (E2E NLG Task)					
	CoLA	SST-2	MRPC	STS-B	QQP	MNLI	QNLI	RTE	Avg.	BLEU	NIST	METEOR	ROUGE	CIDEr	Avg.
FedAvg	28.36	81.08	71.45	87.07	73.24	68.43	65.26	52.17	65.88	0.5878	8.0645	0.4123	0.6405	1.7848	2.2980
FedBitFit	4.65	70.30	69.49	71.64	62.02	43.45	59.82	45.90	53.41	0.5570	7.3859	0.3443	0.5917	1.4059	2.0570
FedLoRA	6.31	70.49	68.38	78.40	68.97	41.97	58.97	43.07	54.57	0.5402	7.0344	0.3625	0.5857	1.3712	1.9788
SLoRA	21.82	72.44	69.00	80.35	69.08	53.26	60.68	50.97	59.70	0.5700	7.9592	0.4001	0.6243	1.7322	2.2572
LEFF	27.74	79.30	70.00	85.00	70.83	62.75	63.24	51.89	63.84	0.5799	8.0296	0.4064	0.6346	1.7521	2.2805

5.2.2 Effect of Compression Ratio

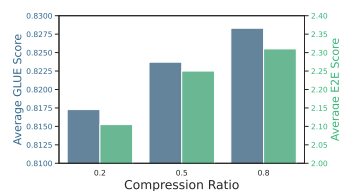


Figure 5: Average scores of LEFF on GLUE benchmark and E2E NLG dataset at different compression rates.

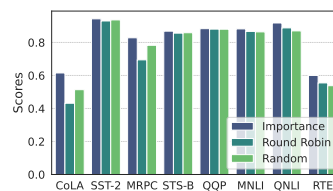


Figure 6: Scores of LEFF on GLUE benchmark using different sampling method.

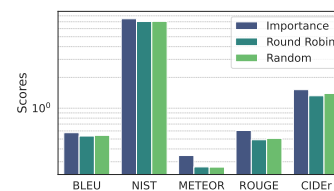


Figure 7: Scores of LEFF on E2E NLG dataset using different sampling method.

We analyze the sensitivity of LEFF’s performance to the compression ratio r . Figure 5 shows that LEFF achieves superior performance with higher values of r (i.e., lower compression levels where more parameters are retained). With higher r , the student model retains more parameters, enhancing its representational capacity to emulate the teacher model more effectively. This, in turn, provides a more precise training context for the local model. Conversely, lower values of r (i.e., higher compression levels) indicate the student model retains fewer parameters, thereby constraining its representational capacity. This leads to less accurate teacher emulation and subsequently degrades LEFF’s training efficacy and overall performance.

5.2.3 Effect of Client Scale

We evaluated model performance across a range of federated clients (8 to 40) on tasks from the GLUE benchmark and for NLG. Our results reveal a systematic degradation in performance as the number of clients increases. As detailed in Table 2, for GLUE tasks, the robustness to client scaling varied significantly across different metrics. For instance, SST-2 demonstrated minimal degradation, with performance decreasing by 3.10% (from 94.30 to 91.38). In contrast, CoLA exhibited substantial sensitivity, with its score declining by 49.18% (from 61.51 to 31.26). Consequently, the average GLUE score dropped from 81.73 to 72.37. NLG tasks, presented in Table 3, showed greater resilience. BLEU scores experienced a marginal reduction of 1.94% (from 0.5762 to 0.5650), while CIDEr registered the largest relative decline at 5.16% (from 1.5174 to 1.4391). These findings suggest that while the model can maintain reasonable efficacy in federated settings with fewer clients, its performance is challenged when scaling to larger client populations.

Table 2: Test result of DeBERTaV3 trained under different client scales.

	Number of Clients				
	8	16	24	32	40
CoLA	61.51	50.21	44.87	35.60	31.26
SST-2	94.30	93.77	93.15	92.30	91.38
MRPC	82.82	77.38	71.44	68.38	64.38
STS-B	86.84	85.90	85.12	80.39	79.35
QQP	88.35	87.32	86.76	86.32	86.00
MNLI	88.20	88.07	87.57	87.36	86.52
QNLI	91.79	91.09	90.45	89.45	89.20
RTE	60.01	59.33	57.16	52.71	50.90
Average	81.73	79.13	77.07	74.06	72.37

5.2.4 Effect of Sampling Methods

We evaluate LEFF employing three distinct sampling strategies: importance-based, round-robin (sequential block fine-tuning per communication round), and random (arbitrary block selection per round). As illustrated in Figure 6 and Figure 7, the importance-based sampling strategy consistently outperforms the round-robin and random strategies across metrics from both the GLUE and E2E NLG benchmarks. On the GLUE benchmark, this performance advantage is particularly pronounced on challenging tasks such as CoLA. Similar trends are observed for MRPC and RTE, although the performance gap diminishes for tasks where all methods achieve high scores. For tasks within the E2E NLG benchmark, importance-based sampling demonstrates consistent superiority, yielding substantial improvements in METEOR and CIDEr scores, alongside modest gains in BLEU and NIST metrics. These results underscore its effectiveness across diverse natural language tasks.

Table 3: Test result of GPT-2 trained under different client scales.

	Number of Clients				
	8	16	24	32	40
BLEU	0.5762	0.5728	0.5726	0.5715	0.5650
NIST	7.4802	7.2763	7.2368	7.1747	6.8036
METEOR	0.3448	0.3401	0.3384	0.3352	0.3275
ROUGE	0.6056	0.6042	0.6033	0.6018	0.5981
CIDEr	1.5174	1.5139	1.5086	1.4988	1.4391
Average	2.1048	2.0615	2.0519	2.0364	1.9467

6 Conclusion

This paper introduced LEFF, a novel federated fine-tuning approach for LLMs that employs selective layer-wise fine-tuning to balance computational efficiency and model performance, achieving a theoretical convergence rate of $\mathcal{O}(1/\sqrt{T})$. Experimental evaluations on the GLUE benchmark and E2E NLG challenge demonstrate LEFF’s performance is comparable to full fine-tuning and surpasses other parameter-efficient methods, highlighting its efficacy for resource-constrained, heterogeneous environments. Despite these strengths, LEFF’s layer selection and compression introduce an inherent efficiency-fidelity trade-off and an approximation error ($\bar{\Delta}^2$) that can cap performance, as indicated by our theory. Additionally, LEFF increases server-side computational load for tasks like layer importance calculation and specialized aggregation, and can incur substantial server-to-client communication for customized model components, particularly with lighter compression. Future research could mitigate these limitations by developing more sophisticated adaptive compression strategies, optimizing server-side operations, or exploring alternative proxy data utilization methods.

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A Proof of Lemma 1

A.1 Bound on the Expected Local Gradient Norm

Proof. We use the standard variance decomposition $\mathbb{E}[\|X\|^2] = \mathbb{E}[\|X - \mathbb{E}[X]\|^2] + \|\mathbb{E}[X]\|^2$.

$$\mathbb{E}_\xi [\|G_{i,t,k}\|^2] = \mathbb{E}_\xi [\|G_{i,t,k} - \mathbb{E}_\xi[G_{i,t,k}]\|^2] + \|\mathbb{E}_\xi[G_{i,t,k}]\|^2. \quad (19)$$

By definition, $\mathbb{E}_\xi[G_{i,t,k}] = \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{i,t,k}^{\mathcal{L}_i} | \check{\Theta}_{g,t}^{\mathcal{L}_i^-})$. The first term is the variance of the stochastic gradient given the current local model $\Theta_{i,t,k}^{\mathcal{L}_i}$ and the (potentially compressed) non-updated parameters $\check{\Theta}_{g,t}^{\mathcal{L}_i^-}$. Assumption 2 provides a bound on the variance of the gradient for the full model: $\mathbb{E}_\xi[\|\nabla \mathcal{F}_i(\Theta; \xi) - \nabla \mathcal{F}_i(\Theta)\|^2] \leq \sigma_i^2 \leq \sigma^2$. We assume this bound also applies to the variance of the stochastic gradient computed only for the selected layers $\mathcal{L}_i$:

$$\mathbb{E}_\xi [\|G_{i,t,k} - \mathbb{E}_\xi[G_{i,t,k}]\|^2] \leq \sigma^2 \quad (20)$$

For the second term, the squared norm of the expected gradient, we use the inequality $\|a + b\|^2 \leq 2\|a\|^2 + 2\|b\|^2$:

$$\begin{aligned} \|\mathbb{E}_\xi[G_{i,t,k}]\|^2 &= \left\| \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{i,t,k}^{\mathcal{L}_i} | \check{\Theta}_{g,t}^{\mathcal{L}_i^-}) \right\|^2 \\ &= \left\| \left(\nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{i,t,k}^{\mathcal{L}_i} | \check{\Theta}_{g,t}^{\mathcal{L}_i^-}) - \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right) + \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right\|^2 \\ &\leq 2 \left\| \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{i,t,k}^{\mathcal{L}_i} | \check{\Theta}_{g,t}^{\mathcal{L}_i^-}) - \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right\|^2 + 2 \left\| \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right\|^2 \end{aligned} \quad (21)$$

The first term in (21) captures the deviation of the expected local gradient at step k from the true local gradient (for layers $\mathcal{L}_i$) evaluated at the round's initial global model $\Theta_{g,t}$. This deviation arises from both the drift of the local model ($\Theta_{i,t,k}^{\mathcal{L}_i}$ vs $\Theta_{g,t}^{\mathcal{L}_i}$) and the use of potentially approximated parameters ($\check{\Theta}_{g,t}^{\mathcal{L}_i^-}$). Assumption 4 bounds the average deviation over K steps: $\mathbb{E}_{\mathcal{L}_i \sim \mathbf{p}_i} [\|\bar{G}_{i,t} - \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t})\|^2] \leq \Delta_{i,t}^2$, where $\bar{G}_{i,t} = (1/K) \sum_{k=0}^{K-1} \mathbb{E}_\xi[G_{i,t,k}]$. While Assumption 4 applies to the average, analyses often rely on bounding the instantaneous deviation. We make a simplifying assumption, that the expected instantaneous deviation (over $\mathcal{L}_i$) is also related to the average approximation error bound Δ_t^2 . Specifically, we assume:

$$\mathbb{E}_{\mathcal{L}_i \sim \mathbf{p}_i} \left[\left\| \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{i,t,k}^{\mathcal{L}_i} | \check{\Theta}_{g,t}^{\mathcal{L}_i^-}) - \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right\|^2 \right] \leq c_a \Delta_t^2 \quad (22)$$

for some constant $c_a \geq 1$.

Combining (20), (21), and (22), and taking expectation over $\mathcal{L}_i \sim \mathbf{p}_i$:

$$\begin{aligned} &\mathbb{E}_{\mathcal{L}_i} \mathbb{E}_\xi [\|G_{i,t,k}\|^2] \\ &\leq \mathbb{E}_{\mathcal{L}_i} [\sigma^2 + \|\mathbb{E}_\xi[G_{i,t,k}]\|^2] \\ &\leq \sigma^2 + \mathbb{E}_{\mathcal{L}_i} \left[2 \left\| \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{i,t,k}^{\mathcal{L}_i} | \check{\Theta}_{g,t}^{\mathcal{L}_i^-}) - \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right\|^2 + 2 \left\| \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right\|^2 \right] \\ &\leq \sigma^2 + 2c_a \Delta_t^2 + 2\mathbb{E}_{\mathcal{L}_i} [\left\| \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right\|^2] \\ &\leq c_b (\sigma^2 + \Delta_t^2 + \mathbb{E}_{\mathcal{L}_i} [\left\| \nabla_{\Theta^{\mathcal{L}_i}} \mathcal{F}_i(\Theta_{g,t}) \right\|^2]) \end{aligned} \quad (23)$$

where $c_b = 2c_a$ is a constant. $\square$

A.2 Bound on the Global Model Update Norm

Proof. The squared norm of the global model change is the sum of the squared norms of the changes in each layer:

$$\mathbb{E} [\|\Theta_{g,t+1} - \Theta_{g,t}\|^2] = \mathbb{E} \left[\sum_{l=1}^L \|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2 \right] = \sum_{l=1}^L \mathbb{E} [\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2], \quad (24)$$

where $\Theta_{g,t}^l$ denotes the parameters of the l -th layer of the global model at round t .

The global model update for layer l at round $t+1$ is given by the weighted average of the corresponding layer parameters from clients that updated this layer:

$$\Theta_{g,t+1}^l = \sum_{i \in \mathcal{S}_t^l} w_i^l \Theta_{i,t,K}^l, \quad (25)$$

where $\mathcal{S}_t^l = \{i \in \mathcal{A}_t \mid l \in \mathcal{L}_i\}$ is the set of clients selected in round t ($\mathcal{A}_t$) that included layer l in their layer block $\mathcal{L}_i$, $w_i^l = D_i / (\sum_{j \in \mathcal{S}_t^l} D_j)$ are the aggregation weights (with $\sum_{i \in \mathcal{S}_t^l} w_i^l = 1$, $w_i^l \geq 0$), and $\Theta_{i,t,K}^l$ is the l -th layer parameter of client i after K local steps starting from $\Theta_{i,t,0}^l = \Theta_{g,t}^l$.

The local update process for layer l on client i (if $l \in \mathcal{L}_i$) follows:

$$\Theta_{i,t,K}^l = \Theta_{i,t,0}^l - \eta \sum_{k=0}^{K-1} G_{i,t,k}^l = \Theta_{g,t}^l - \eta \sum_{k=0}^{K-1} G_{i,t,k}^l, \quad (26)$$

where $G_{i,t,k}^l$ is the component of the stochastic gradient $G_{i,t,k}$ (computed by client i at local step k using data sample $\xi_{i,t,k}$) corresponding to layer l .

Therefore, the change in the global model's l -th layer is:

$$\Theta_{g,t+1}^l - \Theta_{g,t}^l = \sum_{i \in \mathcal{S}_t^l} w_i^l (\Theta_{i,t,K}^l - \Theta_{g,t}^l) = -\eta \sum_{i \in \mathcal{S}_t^l} w_i^l \left(\sum_{k=0}^{K-1} G_{i,t,k}^l \right). \quad (27)$$

We want to bound the expected squared norm $\mathbb{E}[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2]$. Let $\delta_{i,t}^l = \Theta_{i,t,K}^l - \Theta_{g,t}^l = -\eta \sum_{k=0}^{K-1} G_{i,t,k}^l$ denote the total update applied by client i to layer l (if $l \in \mathcal{L}_i$).

$$\mathbb{E}[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2] = \mathbb{E} \left[\left\| \sum_{i \in \mathcal{S}_t^l} w_i^l \delta_{i,t}^l \right\|^2 \right]. \quad (28)$$

The expectation $\mathbb{E}[\cdot]$ is over all sources of randomness: $\mathcal{A}_t$, $\{\mathcal{L}_i\}_{i \in \mathcal{A}_t}$, and $\{\xi_{i,t,k}\}_{i \in \mathcal{A}_t, 0 \leq k < K}$.

Since $\|\cdot\|^2$ is a convex function and $\sum_{i \in \mathcal{S}_t^l} w_i^l = 1$ with $w_i^l \geq 0$, we can apply Jensen's inequality:

$$\left\| \sum_{i \in \mathcal{S}_t^l} w_i^l \delta_{i,t}^l \right\|^2 \leq \sum_{i \in \mathcal{S}_t^l} w_i^l \|\delta_{i,t}^l\|^2. \quad (29)$$

Taking the expectation over all randomness:

$$\mathbb{E}[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2] \leq \mathbb{E} \left[\sum_{i \in \mathcal{S}_t^l} w_i^l \|\delta_{i,t}^l\|^2 \right]. \quad (30)$$

We can rewrite the expectation using the law of total expectation, conditioning first on the client and layer selections ($\mathcal{A}_t, \mathcal{L}_i$), which determines the set $\mathcal{S}_t^l$ and weights w_i^l :

$$\mathbb{E}[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2] \leq \mathbb{E}_{\mathcal{A}_t, \mathcal{L}_i} \left[\sum_{i \in \mathcal{S}_t^l} w_i^l \mathbb{E}_{\xi} [\|\delta_{i,t}^l\|^2 \mid \mathcal{A}_t, \mathcal{L}_i] \right], \quad (31)$$

where $\mathbb{E}_{\xi}[\cdot \mid \mathcal{A}_t, \mathcal{L}_i]$ denotes the expectation over the stochasticity of local gradients $\{\xi_{i,t,k}\}$ given the client and layer selections. Note that the condition $i \in \mathcal{S}_t^l$ implies $i \in \mathcal{A}_t$ and $l \in \mathcal{L}_i$.

Now, we bound the inner term $\mathbb{E}_{\xi}[\|\delta_{i,t}^l\|^2 \mid \mathcal{A}_t, \mathcal{L}_i]$ for $i \in \mathcal{S}_t^l$:

$$\mathbb{E}_{\xi}[\|\delta_{i,t}^l\|^2 \mid \mathcal{A}_t, \mathcal{L}_i] = \mathbb{E}_{\xi} \left[\left\| -\eta \sum_{k=0}^{K-1} G_{i,t,k}^l \right\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right] = \eta^2 \mathbb{E}_{\xi} \left[\left\| \sum_{k=0}^{K-1} G_{i,t,k}^l \right\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right]. \quad (32)$$

Using the standard bound $\mathbb{E}[\|\sum_{k=0}^{K-1} X_k\|^2] \leq K \sum_{k=0}^{K-1} \mathbb{E}[\|X_k\|^2]$ (often used in FL analysis Karimireddy et al. (2020)):

$$\mathbb{E}_\xi \left[\left\| \sum_{k=0}^{K-1} G_{i,t,k}^l \right\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right] \leq K \sum_{k=0}^{K-1} \mathbb{E}_\xi \left[\|G_{i,t,k}^l\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right]. \quad (33)$$

Since $G_{i,t,k}^l$ is the l -th layer component of the full gradient $G_{i,t,k}$, we have $\|G_{i,t,k}^l\|^2 \leq \|G_{i,t,k}\|^2$. Thus:

$$\mathbb{E}_\xi \left[\|G_{i,t,k}^l\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right] \leq \mathbb{E}_\xi \left[\|G_{i,t,k}\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right]. \quad (34)$$

From Assumptions 1, 2, and 4, the expected squared norm of the stochastic gradient $G_{i,t,k}$ computed by client i at local step k can be bounded. A common bound derived under these assumptions in (23) takes the form:

$$\mathbb{E}_\xi \left[\|G_{i,t,k}\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right] \leq C_{\text{grad}} \left(\sigma^2 + \Delta_t^2 + \|\nabla \mathcal{F}_i(\Theta_{g,t})\|^2 \right), \quad (35)$$

where C_{grad} is a constant, and we use $\Theta_{g,t}$ as a reference point, absorbing dependencies on the intermediate local models $\Theta_{i,t,k}$ into the constant C_{grad} (this is a common simplification in FL analysis, valid for sufficiently small ηK). Let $X_{i,t} = \sigma^2 + \Delta_t^2 + \|\nabla \mathcal{F}_i(\Theta_{g,t})\|^2$. Then:

$$\mathbb{E}_\xi \left[\|G_{i,t,k}^l\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right] \leq C_{\text{grad}} X_{i,t}. \quad (36)$$

Substituting back:

$$\mathbb{E}_\xi \left[\|\delta_{i,t}^l\|^2 \mid \mathcal{A}_t, \mathcal{L}_i \right] \leq \eta^2 K \sum_{k=0}^{K-1} (C_{\text{grad}} X_{i,t}) = \eta^2 K^2 C_{\text{grad}} X_{i,t}. \quad (37)$$

Now, substitute this into the bound for $\mathbb{E}[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2]$:

$$\begin{aligned} \mathbb{E} \left[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2 \right] &\leq \mathbb{E}_{\mathcal{A}_t, \mathcal{L}_i} \left[\sum_{i \in \mathcal{S}_t^l} w_i^l (\eta^2 K^2 C_{\text{grad}} X_{i,t}) \right] \\ &= \eta^2 K^2 C_{\text{grad}} \mathbb{E}_{\mathcal{A}_t, \mathcal{L}_i} \left[\sum_{i \in \mathcal{S}_t^l} w_i^l \left(\sigma^2 + \Delta_t^2 + \|\nabla \mathcal{F}_i(\Theta_{g,t})\|^2 \right) \right] \end{aligned} \quad (38)$$

Let $\mathbb{E}_{\mathcal{S}_t^l}[\cdot]$ denote the expectation $\mathbb{E}_{\mathcal{A}_t, \mathcal{L}_i}[\cdot]$. The term $\mathbb{E}_{\mathcal{S}_t^l}[\sum_{i \in \mathcal{S}_t^l} w_i^l(\cdot)]$ represents the expected weighted average over clients participating in the update for layer l . Under assumptions of unbiased client sampling (e.g., uniform random sampling of $\mathcal{A}_t$ clients) and potentially layer sampling ($\mathcal{L}_i$), this expectation can be related to the average over all clients. Assuming there exists a constant c_d (which may depend on the sampling strategy, e.g., A/N , and the distribution of weights w_i^l) such that:

$$\mathbb{E}_{\mathcal{S}_t^l} \left[\sum_{i \in \mathcal{S}_t^l} w_i^l X_{i,t} \right] \leq c_d \frac{1}{N} \sum_{i=1}^N X_{i,t}. \quad (39)$$

Then:

$$\begin{aligned} \mathbb{E} \left[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2 \right] &\leq \eta^2 K^2 C_{\text{grad}} c_d \frac{1}{N} \sum_{i=1}^N \left(\sigma^2 + \Delta_t^2 + \|\nabla \mathcal{F}_i(\Theta_{g,t})\|^2 \right) \\ &= \eta^2 K^2 C_{\text{grad}} c_d \left(\sigma^2 + \Delta_t^2 + \frac{1}{N} \sum_{i=1}^N \|\nabla \mathcal{F}_i(\Theta_{g,t})\|^2 \right). \end{aligned} \quad (40)$$

Now we use Assumption 3 (Bounded Heterogeneity): $\frac{1}{N} \sum_{i=1}^N \|\nabla \mathcal{F}_i(\Theta) - \nabla \mathcal{F}(\Theta)\|^2 \leq \zeta^2$. We have the decomposition:

$$\begin{aligned}
\frac{1}{N} \sum_{i=1}^N \|\nabla \mathcal{F}_i(\Theta_{g,t})\|^2 &= \frac{1}{N} \sum_{i=1}^N \|\nabla \mathcal{F}_i(\Theta_{g,t}) - \nabla \mathcal{F}(\Theta_{g,t}) + \nabla \mathcal{F}(\Theta_{g,t})\|^2 \\
&= \frac{1}{N} \sum_{i=1}^N (\|\nabla \mathcal{F}_i(\Theta_{g,t}) - \nabla \mathcal{F}(\Theta_{g,t})\|^2 + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2 + 2\langle \nabla \mathcal{F}_i(\Theta_{g,t}) - \nabla \mathcal{F}(\Theta_{g,t}), \nabla \mathcal{F}(\Theta_{g,t}) \rangle) \\
&= \left(\frac{1}{N} \sum_{i=1}^N \|\nabla \mathcal{F}_i(\Theta_{g,t}) - \nabla \mathcal{F}(\Theta_{g,t})\|^2 \right) + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2 \\
&\quad + 2 \left\langle \frac{1}{N} \sum_{i=1}^N \nabla \mathcal{F}_i(\Theta_{g,t}) - \nabla \mathcal{F}(\Theta_{g,t}), \nabla \mathcal{F}(\Theta_{g,t}) \right\rangle.
\end{aligned} \tag{41}$$

Since $\nabla \mathcal{F}(\Theta_{g,t}) = \frac{1}{N} \sum_{i=1}^N \nabla \mathcal{F}_i(\Theta_{g,t})$, the cross term is zero. Using Assumption 3:

$$\frac{1}{N} \sum_{i=1}^N \|\nabla \mathcal{F}_i(\Theta_{g,t})\|^2 \leq \zeta^2 + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2. \tag{42}$$

Substituting this into the bound for the layer update:

$$\mathbb{E} \left[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2 \right] \leq \eta^2 K^2 C_{\text{grad}} c_d (\sigma^2 + \Delta_t^2 + \zeta^2 + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2). \tag{43}$$

Finally, sum over all layers $l = 1, \dots, L$:

$$\begin{aligned}
\mathbb{E} \left[\|\Theta_{g,t+1} - \Theta_{g,t}\|^2 \right] &= \sum_{l=1}^L \mathbb{E} \left[\|\Theta_{g,t+1}^l - \Theta_{g,t}^l\|^2 \right] \\
&\leq \sum_{l=1}^L [\eta^2 K^2 C_{\text{grad}} c_d (\sigma^2 + \Delta_t^2 + \zeta^2 + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2)] \\
&= L \eta^2 K^2 C_{\text{grad}} c_d (\sigma^2 + \Delta_t^2 + \zeta^2 + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2)
\end{aligned} \tag{44}$$

Let $C_3 = L C_{\text{grad}} c_d$. This constant incorporates the number of layers L , the constant from the gradient bound C_{grad} , and the constant related to sampling and weighting c_d . This yields the final result:

$$\mathbb{E} \left[\|\Theta_{g,t+1} - \Theta_{g,t}\|^2 \right] \leq C_3 \eta^2 K^2 (\sigma^2 + \Delta_t^2 + \zeta^2 + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2). \tag{45}$$

This completes the proof. $\square$

B Proof of Main Theorem

Proof. In this section, we present the convergence analysis for our algorithm. Our goal is to bound the average squared norm of the global gradient over T communication rounds.

We begin with the L -smoothness property of the global objective function $\mathcal{F}$, stated in **Assumption 1**. By the definition of L -smoothness, often referred to as the Descent Lemma or Quadratic Upper Bound, we have:

$$\mathbb{E}[\mathcal{F}(\Theta_{g,t+1})] \leq \mathcal{F}(\Theta_{g,t}) + \mathbb{E}[\langle \nabla \mathcal{F}(\Theta_{g,t}), \Theta_{g,t+1} - \Theta_{g,t} \rangle] + \frac{L}{2} \mathbb{E}[\|\Theta_{g,t+1} - \Theta_{g,t}\|^2], \tag{46}$$

where the expectation $\mathbb{E}[\cdot]$ is taken over all sources of randomness up to round $t+1$, including client sampling ($\mathcal{A}_t$), layer sampling ($\mathcal{L}_i$ for $i \in \mathcal{A}_t$), and local stochastic gradient noise ($\xi_{i,t,k}$).

The core of the analysis involves carefully bounding the inner product term $\mathbb{E}[\langle \nabla \mathcal{F}(\Theta_{g,t}), \Theta_{g,t+1} - \Theta_{g,t} \rangle]$ and the quadratic term $\mathbb{E}[\|\Theta_{g,t+1} - \Theta_{g,t}\|^2]$. The bound for the quadratic term is typically established in a separate lemma (referred to as **Lemma 1**). We focus on deriving the bound for the inner product term.

B.1 Bounding the Inner Product Term

Recall the global model update is constructed layer-wise:

$$\Theta_{g,t+1} - \Theta_{g,t} = \{\Theta_{g,t+1}^l - \Theta_{g,t}^l\}_{l=1\dots L} \quad (47)$$

where for each layer l :

$$\Theta_{g,t+1}^l - \Theta_{g,t}^l = -\eta \sum_{i \in \mathcal{S}_t^l} w_i^l \sum_{k=0}^{K-1} G_{i,t,k}^l \quad (48)$$

Here, $\mathcal{S}_t^l = \{i \in \mathcal{A}_t \mid l \in \mathcal{L}_i\}$ is the set of selected clients that update layer l , w_i^l is the aggregation weight for client i on layer l , and $G_{i,t,k}^l$ is the stochastic gradient computed by client i for layer l at local step k .

The inner product term can be expanded as a sum over layers:

$$\begin{aligned} \mathbb{E}[\langle \nabla \mathcal{F}(\Theta_{g,t}), \Theta_{g,t+1} - \Theta_{g,t} \rangle] &= \mathbb{E} \left[\sum_{l=1}^L \langle \nabla_{\Theta^l} \mathcal{F}(\Theta_{g,t}), \Theta_{g,t+1}^l - \Theta_{g,t}^l \rangle \right] \\ &= \sum_{l=1}^L \mathbb{E} \left[\langle \nabla_{\Theta^l} \mathcal{F}(\Theta_{g,t}), -\eta \sum_{i \in \mathcal{S}_t^l} w_i^l \sum_{k=0}^{K-1} G_{i,t,k}^l \rangle \right] \\ &= -\sum_{l=1}^L \eta \mathbb{E} \left[\langle \nabla_{\Theta^l} \mathcal{F}(\Theta_{g,t}), \sum_{i \in \mathcal{S}_t^l} w_i^l \sum_{k=0}^{K-1} G_{i,t,k}^l \rangle \right] \end{aligned} \quad (49)$$

Let $\mathbb{E}_\xi[\cdot]$ denote the expectation over the local data samples ξ , conditioned on the client selection $\mathcal{A}_t$ and layer selections $\mathcal{L}_i$. Let $\bar{G}_{i,t}^l = \frac{1}{K} \sum_{k=0}^{K-1} \mathbb{E}_\xi[G_{i,t,k}^l | \mathcal{A}_t, \mathcal{L}_i]$ be the average expected local gradient for layer l computed by client i (if $l \in \mathcal{L}_i$). Then $\sum_{k=0}^{K-1} \mathbb{E}_\xi[G_{i,t,k}^l | \mathcal{A}_t, \mathcal{L}_i] = K \bar{G}_{i,t}^l$. Taking the expectation over ξ first, we get:

$$\begin{aligned} \mathbb{E}[\langle \cdots \rangle] &= -\sum_{l=1}^L \eta \mathbb{E}_{\mathcal{A}_t, \mathcal{L}_i} \left[\langle \nabla_{\Theta^l} \mathcal{F}(\Theta_{g,t}), \sum_{i \in \mathcal{S}_t^l} w_i^l K \bar{G}_{i,t}^l \rangle \right] \\ &= -K \sum_{l=1}^L \eta \mathbb{E} \left[\langle \nabla_{\Theta^l} \mathcal{F}(\Theta_{g,t}), \sum_{i \in \mathcal{S}_t^l} w_i^l \bar{G}_{i,t}^l \rangle \right] \end{aligned} \quad (50)$$

where the outer expectation $\mathbb{E}[\cdot]$ is now over $\mathcal{A}_t$ and $\mathcal{L}_i$.

Standard techniques in FL analysis (e.g., using algebraic identities like $2\langle a, b \rangle = \|a\|^2 + \|b\|^2 - \|a - b\|^2$ or Young's inequality, and carefully handling the expectations over sampling) allow us to bound the inner product. This involves decomposing the error terms and applying the assumptions. While the detailed derivation is intricate due to the layer selection and weighting scheme, it leads to a bound of the following form (similar to analyses of FedAvg variants):

$$\mathbb{E}[\langle \nabla \mathcal{F}(\Theta_{g,t}), \Theta_{g,t+1} - \Theta_{g,t} \rangle] \leq -C_4 \eta K \|\nabla \mathcal{F}(\Theta_{g,t})\|^2 + C_5 \eta K (\bar{\Delta}_t^2 + \zeta^2 + \sigma^2/K) \quad (51)$$

where $\bar{\Delta}_t^2 = \frac{1}{N} \sum_i \Delta_{i,t}^2$ is the average model approximation error bound across clients at round t . The constants C_4 and C_5 depend on factors like the client sampling ratio (A/N), layer sampling probabilities ($\mathbf{p}_i$), and potentially the distribution of weights w_i^l . The term $-C_4 \eta K \|\nabla \mathcal{F}(\Theta_{g,t})\|^2$ represents the desired descent along the negative gradient direction, while the term $C_5 \eta K (\bar{\Delta}_t^2 + \zeta^2 + \sigma^2/K)$ captures the accumulated error from model approximation, heterogeneity, and residual stochastic gradient variance (scaled by $1/K$ due to averaging K steps implicitly or explicitly in the derivation).

B.2 Completing the Proof

We now substitute the inner product bound (51) and the bound on the quadratic term from **Lemma 1** into the L -smoothness inequality (46). Lemma 1 typically provides a bound like:

$$\mathbb{E}[\|\Theta_{g,t+1} - \Theta_{g,t}\|^2] \leq C_3 \eta^2 K^2 (\sigma^2 + \bar{\Delta}_t^2 + \zeta^2 + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2) \quad (52)$$

where C_3 is another constant derived in Lemma 1.

Substituting (51) and (52) into (46):

$$\begin{aligned}\mathbb{E}[\mathcal{F}(\Theta_{g,t+1})] &\leq \mathcal{F}(\Theta_{g,t}) - C_4\eta K \|\nabla \mathcal{F}(\Theta_{g,t})\|^2 + C_5\eta K (\bar{\Delta}_t^2 + \zeta^2 + \sigma^2/K) \\ &\quad + \frac{L}{2}C_3\eta^2 K^2 (\sigma^2 + \bar{\Delta}_t^2 + \zeta^2 + \|\nabla \mathcal{F}(\Theta_{g,t})\|^2)\end{aligned}\quad (53)$$

Rearranging the terms to group the gradient norm:

$$\begin{aligned}\mathbb{E}[\mathcal{F}(\Theta_{g,t+1})] &\leq \mathcal{F}(\Theta_{g,t}) - \left(C_4\eta K - \frac{LC_3}{2}\eta^2 K^2\right) \|\nabla \mathcal{F}(\Theta_{g,t})\|^2 \\ &\quad + C_5\eta K (\bar{\Delta}_t^2 + \zeta^2 + \sigma^2/K) + \frac{LC_3}{2}\eta^2 K^2 (\sigma^2 + \bar{\Delta}_t^2 + \zeta^2)\end{aligned}\quad (54)$$

To ensure convergence, we require the coefficient of the gradient norm term to be positive. We choose the local learning rate η sufficiently small such that $C_4\eta K - \frac{LC_3}{2}\eta^2 K^2 > 0$. A standard choice is to make the second term at most half of the first term, which holds if $\eta \leq \frac{C_4}{LC_3K}$. Under this condition:

$$C_4\eta K - \frac{LC_3}{2}\eta^2 K^2 \geq C_4\eta K - \frac{LC_3}{2} \left(\frac{C_4}{LC_3K}\right) \eta K = C_4\eta K - \frac{C_4}{2}\eta K = \frac{C_4}{2}\eta K \quad (55)$$

Thus, the inequality becomes:

$$\begin{aligned}\mathbb{E}[\mathcal{F}(\Theta_{g,t+1})] &\leq \mathcal{F}(\Theta_{g,t}) - \frac{C_4}{2}\eta K \|\nabla \mathcal{F}(\Theta_{g,t})\|^2 \\ &\quad + C_6\eta K (\bar{\Delta}_t^2 + \zeta^2 + \sigma^2/K) + C_7\eta^2 K^2 (\sigma^2 + \bar{\Delta}_t^2 + \zeta^2)\end{aligned}\quad (56)$$

where we define $C_6 = C_5$ and $C_7 = LC_3/2$.

Rearranging to isolate the gradient term:

$$\begin{aligned}\frac{C_4}{2}\eta K \mathbb{E}[\|\nabla \mathcal{F}(\Theta_{g,t})\|^2] &\leq \mathcal{F}(\Theta_{g,t}) - \mathbb{E}[\mathcal{F}(\Theta_{g,t+1})] \\ &\quad + C_6\eta K (\bar{\Delta}_t^2 + \zeta^2 + \sigma^2/K) + C_7\eta^2 K^2 (\sigma^2 + \bar{\Delta}_t^2 + \zeta^2)\end{aligned}\quad (57)$$

Summing this inequality over $t = 0, 1, \dots, T-1$:

$$\begin{aligned}\frac{C_4}{2}\eta K \sum_{t=0}^{T-1} \mathbb{E}[\|\nabla \mathcal{F}(\Theta_{g,t})\|^2] &\leq \sum_{t=0}^{T-1} (\mathcal{F}(\Theta_{g,t}) - \mathbb{E}[\mathcal{F}(\Theta_{g,t+1})]) \\ &\quad + \sum_{t=0}^{T-1} [C_6\eta K (\bar{\Delta}_t^2 + \zeta^2 + \sigma^2/K) + C_7\eta^2 K^2 (\sigma^2 + \bar{\Delta}_t^2 + \zeta^2)]\end{aligned}\quad (58)$$

The first term on the right-hand side is a telescoping sum:

$$\sum_{t=0}^{T-1} (\mathcal{F}(\Theta_{g,t}) - \mathbb{E}[\mathcal{F}(\Theta_{g,t+1})]) = \mathcal{F}(\Theta_{g,0}) - \mathbb{E}[\mathcal{F}(\Theta_{g,T})] \quad (59)$$

Assuming the objective function is bounded below by F^* , i.e., $\mathcal{F}(\Theta) \geq F^*$ for all Θ , we have $\mathcal{F}(\Theta_{g,0}) - \mathbb{E}[\mathcal{F}(\Theta_{g,T})] \leq \mathcal{F}(\Theta_{g,0}) - F^*$.

Substituting this back and dividing by T :

$$\begin{aligned}\frac{C_4\eta K}{2T} \sum_{t=0}^{T-1} \mathbb{E}[\|\nabla \mathcal{F}(\Theta_{g,t})\|^2] &\leq \frac{\mathcal{F}(\Theta_{g,0}) - F^*}{T} \\ &\quad + \frac{1}{T} \sum_{t=0}^{T-1} [C_6\eta K (\bar{\Delta}_t^2 + \zeta^2 + \sigma^2/K) + C_7\eta^2 K^2 (\sigma^2 + \bar{\Delta}_t^2 + \zeta^2)]\end{aligned}\quad (60)$$

Finally, dividing by $\frac{C_4\eta K}{2}$ yields the bound on the average squared gradient norm:

$$\begin{aligned} \frac{1}{T} \sum_{t=0}^{T-1} \mathbb{E}[\|\nabla \mathcal{F}(\Theta_{g,t})\|^2] &\leq \frac{2(\mathcal{F}(\Theta_{g,0}) - F^*)}{C_4\eta KT} \\ &\quad + \frac{2C_6}{C_4} \left(\frac{1}{T} \sum_{t=0}^{T-1} \bar{\Delta}_t^2 + \zeta^2 + \frac{\sigma^2}{K} \right) \\ &\quad + \frac{2C_7}{C_4} \eta K \left(\frac{1}{T} \sum_{t=0}^{T-1} (\sigma^2 + \bar{\Delta}_t^2 + \zeta^2) \right) \end{aligned} \quad (61)$$

Let $\bar{\Delta}^2 = \frac{1}{T} \sum_{t=0}^{T-1} \bar{\Delta}_t^2$ be the average model approximation error over T rounds. Define constants $C_8 = 2/C_4$, $C_9 = 2C_6/C_4$, and $C_{10} = 2C_7/C_4$. We arrive at the final convergence result:

$$\frac{1}{T} \sum_{t=0}^{T-1} \mathbb{E}[\|\nabla \mathcal{F}(\Theta_{g,t})\|^2] \leq \underbrace{\frac{C_8(\mathcal{F}(\Theta_{g,0}) - F^*)}{\eta KT}}_{\text{Vanishing term}} + \underbrace{C_9 \left(\bar{\Delta}^2 + \zeta^2 + \frac{\sigma^2}{K} \right) + C_{10}\eta K(\sigma^2 + \bar{\Delta}^2 + \zeta^2)}_{\text{Error floor}} \quad (62)$$

This result shows that the average squared gradient norm converges to an error floor determined by the data heterogeneity (ζ^2), stochastic gradient noise (σ^2/K), average model approximation error ($\bar{\Delta}^2$), and the chosen learning rate (η), at a rate of $\mathcal{O}(1/T)$. $\square$

C Additional Experimental Results and Analyses

This appendix provides supplementary materials and detailed results that support the claims made in the main paper. The content is organized to present further validation of LEFF’s scalability, a comprehensive analysis of client-side overhead, ablation studies on key hyperparameters, and empirical validation of our theoretical convergence claims.

C.1 Scalability to State-of-the-Art Models and Benchmarks

To demonstrate the scalability and effectiveness of LEFF on contemporary large-scale architectures, we extend our evaluation to the Llama-3.1-8B Grattafiori et al. (2024) model using the challenging MMLU benchmark Hendrycks et al. (2021). This experiment includes highly relevant state-of-the-art baselines FLoRA Wang et al. (2024d) and FlexLoRA Bai et al. (2024). As shown in Table 4, LEFF outperforms these recent methods by a significant margin of 1.8-2.3 points on the 5-shot MMLU average. This superior performance is achieved while simultaneously reducing the peak client-side GPU memory by over 36%. These results confirm that LEFF’s design is highly effective and its efficiency benefits are even more pronounced on larger models where client-side resources are the primary bottleneck.

Table 4: Comparison of LEFF with SOTA methods on the Llama-3.1-8B model using the MMLU benchmark (5-shot average accuracy).

Method	MMLU (5-shot Avg.)	Peak GPU Memory (Client)
FlexLoRA	55.7	46.868 GB
FLoRA	55.2	46.868 GB
LEFF	57.5	29.881 GB

C.2 Analysis of Client-Side Computational Overhead

A detailed analysis of the computational overhead on client devices is crucial for evaluating the practical viability of any federated fine-tuning method. We present a comprehensive comparison of the number of trainable parameters and the peak GPU memory usage across various models and algorithms in Table 5. This analysis highlights LEFF’s unique and superior efficiency profile. LEFF drastically reduces peak GPU memory—for instance, achieving a 79% reduction on GPT2-Large

compared to FedAvg and 66% compared to FedLoRA. This is because its architecture selectively loads only the necessary layers into GPU memory, whereas other PEFT methods must load the entire frozen model, resulting in much higher memory footprints. Concurrently, while achieving the lowest memory cost, LEFF deliberately retains more trainable parameters than methods like FedLoRA or FedBitFit. This design maintains greater model expressiveness, which translates to superior task performance. Thus, LEFF strikes an optimal balance, delivering the minimal resource cost for deployment on constrained devices while preserving enough capacity for high-accuracy fine-tuning.

Table 5: Computational cost comparison of different models and algorithms. "OOM" indicates Out of Memory. For Llama-3.1-8B, FedBitFit is not applicable as the model has no bias terms to train.

Model	Algorithm	Trainable Params	Peak Memory (GB)
DeBERTaV3-Base	FedAvg	85,648,130	3.841
DeBERTaV3-Base	FedLoRA	1,340,930	2.644
DeBERTaV3-Base	FedBitFit	102,914	2.198
DeBERTaV3-Base	LEFF	7,681,538	2.136
DeBERTaV3-Base	SLoRA	1,340,930	2.644
DeBERTaV3-Large	FedAvg	303,363,074	9.361
DeBERTaV3-Large	FedLoRA	3,557,378	6.660
DeBERTaV3-Large	FedBitFit	272,386	5.488
DeBERTaV3-Large	LEFF	13,649,922	3.005
DeBERTaV3-Large	SLoRA	3,557,378	6.660
GPT2	FedAvg	85,056,000	3.358
GPT2	FedLoRA	811,008	2.476
GPT2	FedBitFit	102,144	2.206
GPT2	LEFF	7,089,408	1.719
GPT2	SLoRA	811,008	2.476
GPT2-Large	FedAvg	708,390,400	15.548
GPT2-Large	FedLoRA	4,055,040	9.739
GPT2-Large	FedBitFit	508,160	8.318
GPT2-Large	LEFF	19,680,000	3.240
GPT2-Large	SLoRA	4,055,040	9.739
Llama-3.1-8B	FedAvg	OOM	OOM
Llama-3.1-8B	FedLoRA	20,971,520	46.868
Llama-3.1-8B	FedBitFit	No Bias	No Bias
Llama-3.1-8B	LEFF	743,452,672	29.881
Llama-3.1-8B	SLoRA	20,971,520	46.868

C.3 Ablation Study on the Proxy Dataset

The choice of the proxy dataset for knowledge distillation is a key aspect of the LEFF framework. We conduct an ablation study to investigate the sensitivity of our method to this choice. Our distillation objective is designed to be robust by matching intermediate functional representations (hidden states and attention matrices) rather than task-specific knowledge, which should reduce sensitivity to the proxy data's domain. The empirical results on the E2E NLG task, shown in Table 6, confirm this hypothesis. Performance remains remarkably stable across diverse corpora, from the in-domain WebNLG to general-purpose datasets like WikiText-103 and OpenWebText. The minimal fluctuation across all metrics demonstrates that LEFF is not reliant on a perfectly-matched proxy corpus, validating its practical applicability in real-world scenarios where such data may not be readily available.

Table 6: Ablation study on the choice of proxy datasets for the E2E NLG task.

Proxy Dataset	BLEU	NIST	METEOR	ROUGE	CIDEr
WikiText-103	0.5765	8.0012	0.4041	0.6310	1.7450
WebNLG	0.5799	8.0296	0.4064	0.6346	1.7521
OpenWebText	0.5712	7.9688	0.4015	0.6259	1.7345

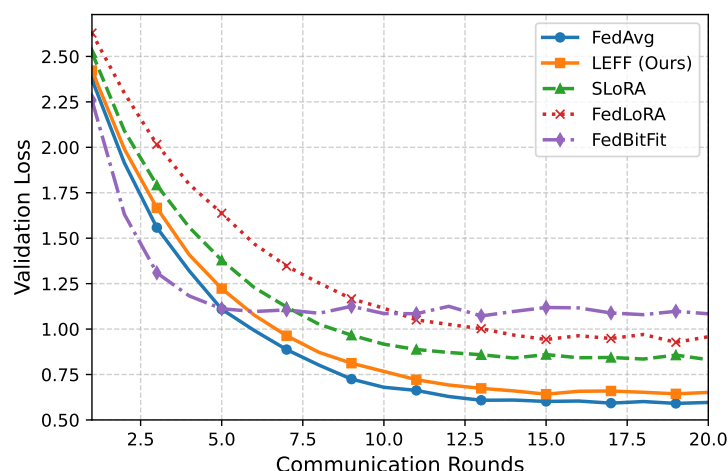


Figure 8: The validation loss convergence curve of different methods under high data heterogeneity ($\alpha = 0.05$).

C.4 Statistical Stability of Results

To ensure the reliability of our findings, we report the standard deviations of our main experimental results across three runs with different random seeds. The results, summarized in Table 7, show that the standard deviations are consistently small across all tasks and methods. This confirms that our method is stable and the reported performance gains are consistent. LEFF exhibits stability comparable to or better than the baselines, substantiating the robustness of our conclusions.

Table 7: Standard deviations of test results for DeBERTaV3 (on GLUE tasks) and GPT2 (on the E2E NLG task) across three runs with different random seeds.

Model	DeBERTaV3 (GLUE Tasks)								GPT2 (E2E NLG Task)				
	CoLA	SST-2	MRPC	STS-B	QQP	MNLI	QNLI	RTE	BLEU	NIST	METEOR	ROUGE	CIDEr
FedAvg	1.52	0.71	0.88	0.45	0.31	0.53	0.62	1.21	0.0041	0.1512	0.0028	0.0033	0.0805
FedBitFit	1.89	0.95	1.02	0.82	0.55	0.98	0.77	1.53	0.0053	0.2144	0.0045	0.0049	0.1231
FedLoRA	1.72	0.88	1.15	0.75	0.49	1.05	0.81	1.68	0.0058	0.2516	0.0041	0.0051	0.1189
SLoRA	1.45	0.81	0.95	0.68	0.42	0.85	0.71	1.35	0.0049	0.1832	0.0035	0.0039	0.0948
LEFF	1.38	0.75	0.91	0.51	0.35	0.62	0.68	1.25	0.0045	0.1604	0.0031	0.0035	0.0882

C.5 Empirical Convergence Analysis

Figure 8 provides an empirical validation of our theoretical convergence analysis presented in Section 4. The validation loss curves for all compared methods were plotted under a high data heterogeneity setting ($\alpha = 0.05$). The results show that LEFF converges stably and efficiently. Its final validation loss is substantially closer to that of full fine-tuning (FedAvg) compared to other PEFT methods like FedLoRA and SLoRA. This empirical evidence supports our theoretical analysis (Theorem 1), demonstrating that LEFF not only converges but also reaches a superior solution in challenging non-IID environments.

D Broader Impacts

D.1 Environmental Cost

The server-side computation in LEFF for layer importance calculation and knowledge distillation represents a trade-off for enabling client-side efficiency. By making fine-tuning feasible on numerous distributed, low-power edge devices, our approach can reduce the overall system’s reliance on large, consistently energy-intensive data centers. This decentralization lowers the barrier to entry for

participation in model training and may lead to a more distributed and potentially more energy-efficient computational footprint compared to fully centralized training paradigms.

D.2 Dual-Use Risks

Making LLM fine-tuning more efficient and accessible could lower the barrier for misuse. However, the federated architecture of LEFF provides a natural control and governance point at the central server. This centralized aggregation step allows for the implementation of safeguards, such as client vetting, anomaly detection in model updates, and monitoring for malicious fine-tuning objectives. Such governance features are largely absent in purely decentralized or local fine-tuning scenarios, providing a mechanism to mitigate potential misuse.